

## Evolution of Quantitative Traits 1



### Outline

- what are quantitative traits
- how many genes
- heritability and additive variance
- measuring selection
- forms of selection

B&D Ch. 9, pp. 294-297, 318-325; box 9.3, 9.4

### Quantitative Traits

continuous traits

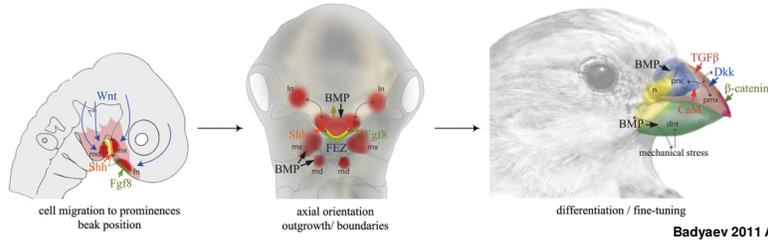


meristic traits



threshold traits

### Evolution of Quantitative Traits



several to many genes may affect phenotype  
-- number, location, identity of genes unknown

environmental variation

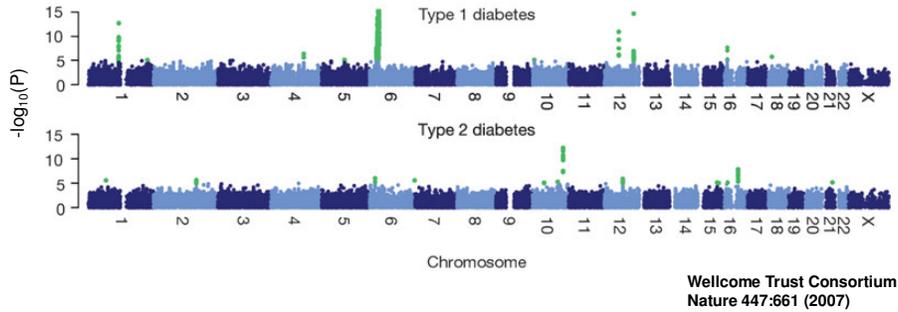
developmental noise



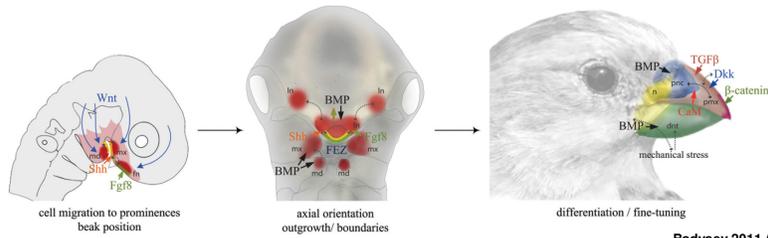
## genetic architecture of quantitative traits

### Genome-Wide Association studies

- genomic SNP map; high throughput sequencing
- survey of large sample from randomly-mating population
- compare affected group (w/disease) and control group



## Evolution of Quantitative Traits



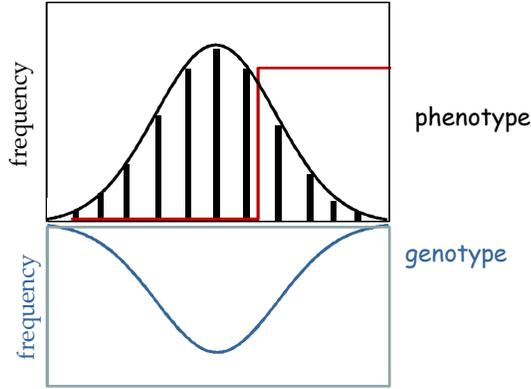
$$P = G + E$$

P = phenotype value (what is measured)

G = genotypic value = expected phenotypic value  
of a given genotype

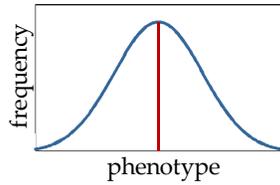
E = environmental deviation

relating phenotypic variation to genetic variation

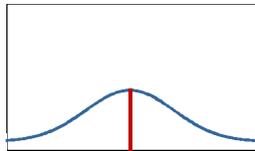


$$P = G + E \rightarrow V_P = V_G + V_E$$

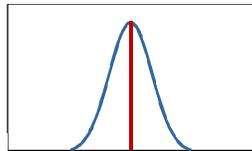
Variance =  $\frac{1}{N} \sum (x_i - \bar{x})^2$



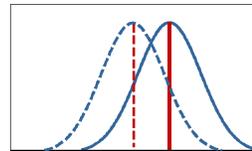
Mean =  $\frac{1}{N} \sum n_i$



same mean,  
larger variance

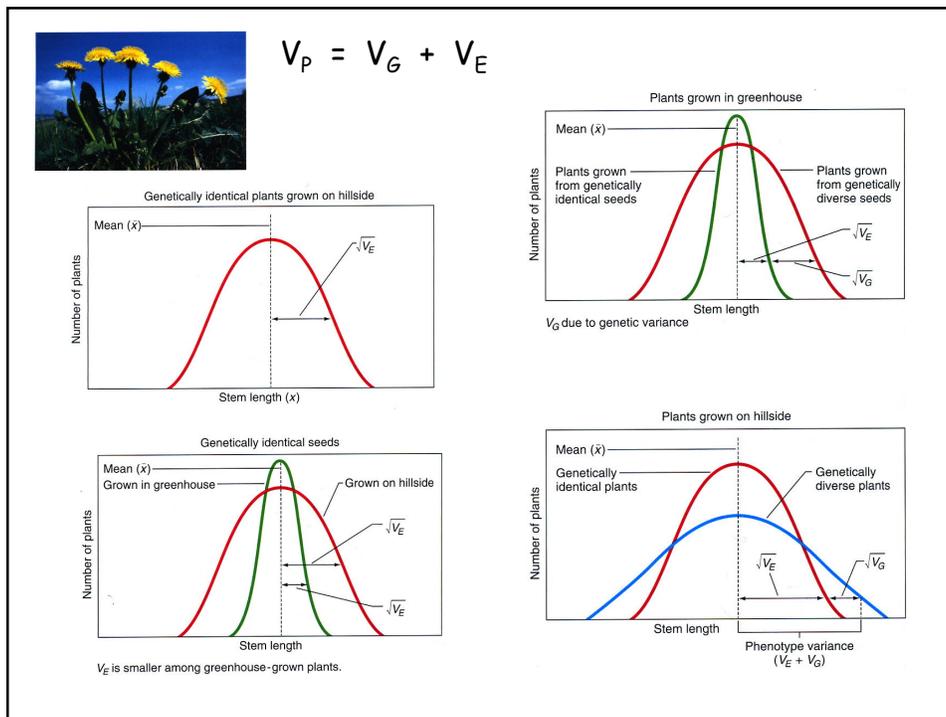


same mean,  
smaller variance



different mean,  
same variance

$$V_P = V_G + V_E$$



heritability and additive genetic variance:

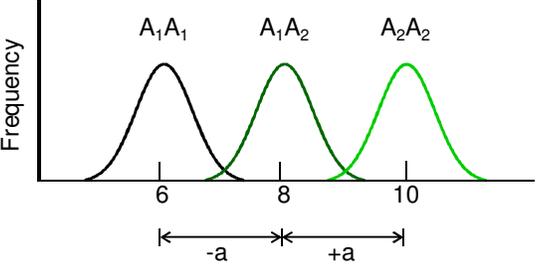
$$V_P = V_G + V_E$$

genetic variance ( $V_G$ ) components:

- $V_A$  - additive genetic variance
- $V_D$  - dominance variance
- $V_I$  - epistatic variance
- $V_M$  - maternal variance

### additive genetic variance, $V_A$

effect of an allele on the phenotype is independent of what other alleles are present

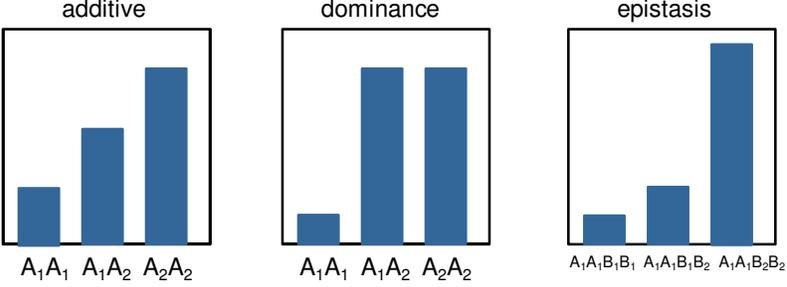


the *HMGA2* locus in human affects height: one allele increases height by 0.5 cm  
(Weedon et al 2007 Nature Genetics 39:1245)

*\*differences due to additive alleles are transmitted from parents to offspring*

### dominance variance ( $V_D$ ) and epistatic variance ( $V_I$ )

dominance and epistasis are interactions between alleles - effect of an allele on the phenotype depends on what allele(s) it is paired with



*\*effects of dominance and epistasis are not inherited*

how can we measure additive genetic variance ( $V_A$ )?

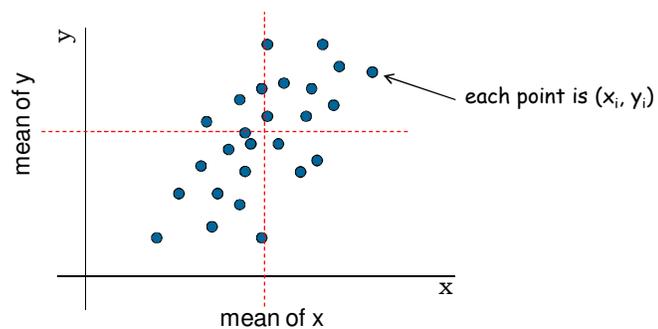
heritability,  $h^2$  is:  
 the proportion of phenotypic variance  
 that is due to additive genetic variance  $\frac{V_A}{V_P} = h^2$

compare trait values in close relatives (parents and offspring)

rear under same environmental conditions - minimize  $V_E$

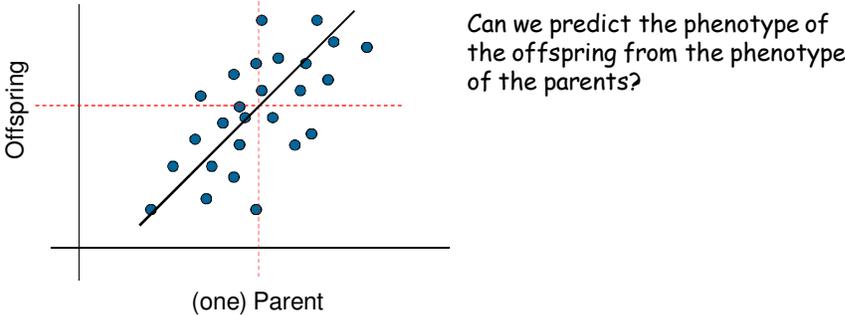
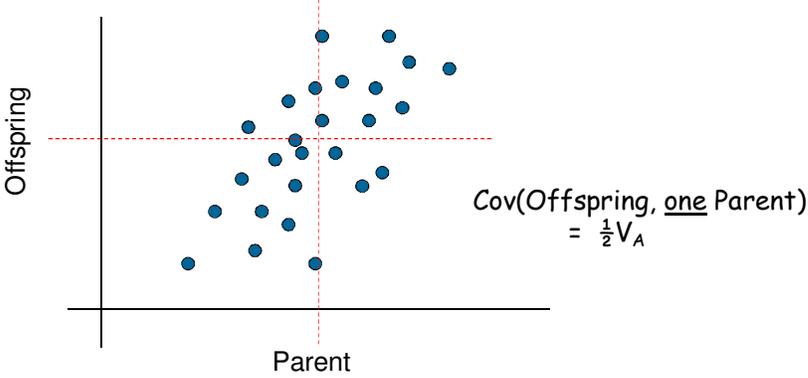
estimate the strength of similarity: P-O regression

### Covariance



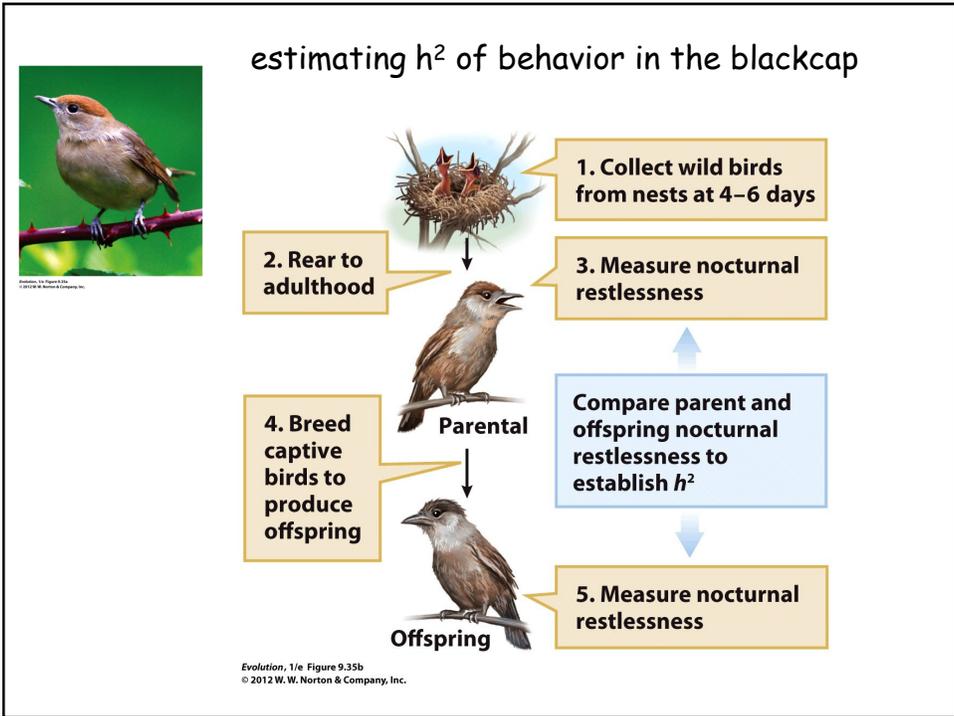
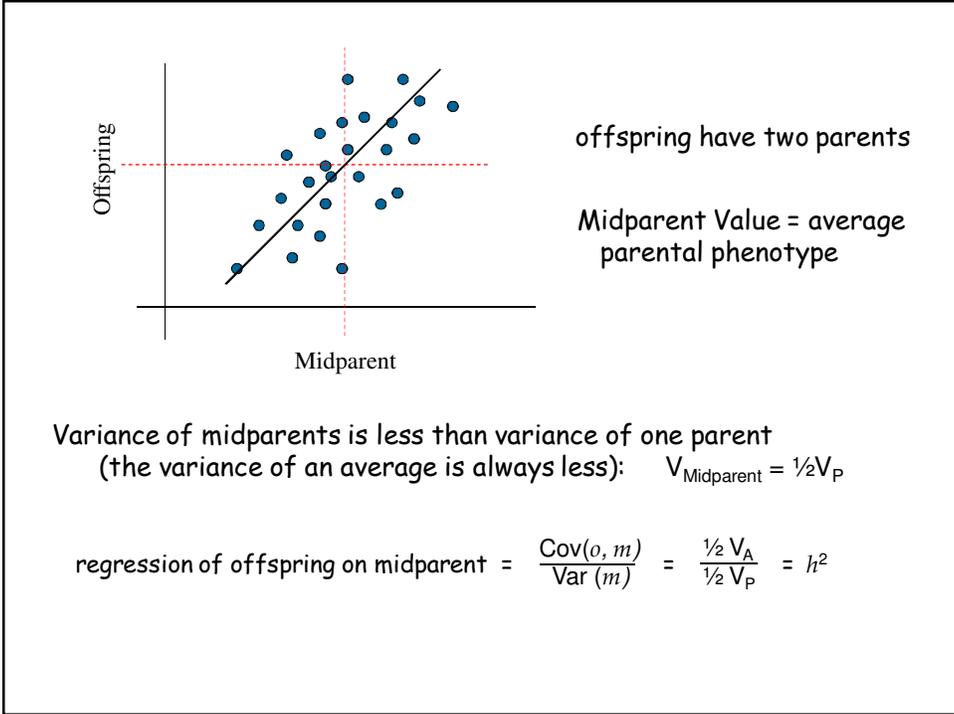
$$\frac{1}{n} \sum_i (x_i - \bar{x})(y_i - \bar{y}) \equiv Cov(x, y)$$

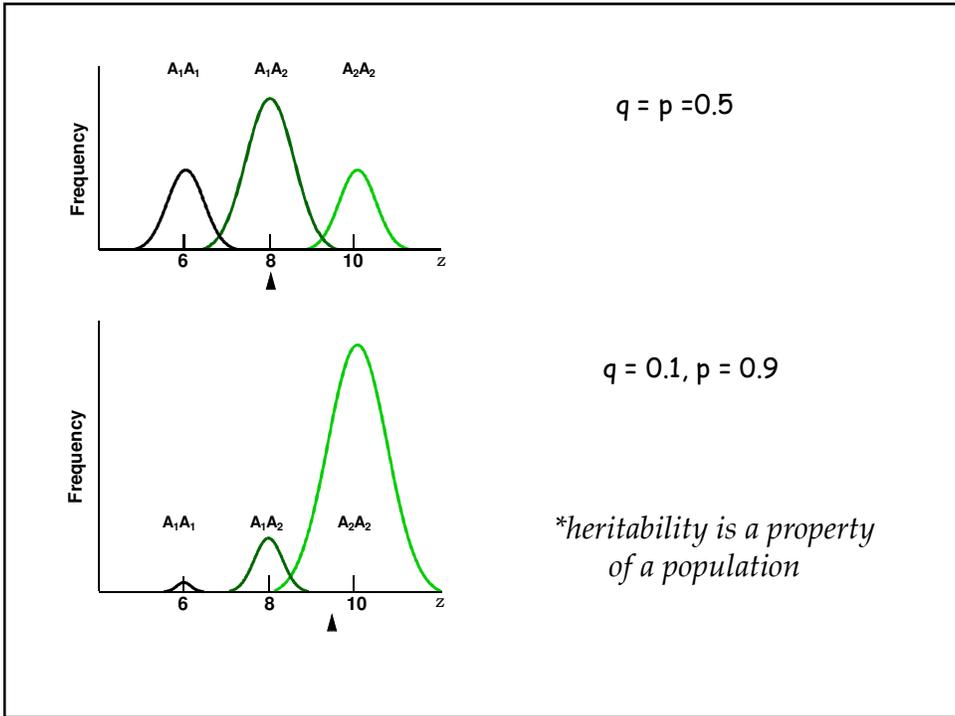
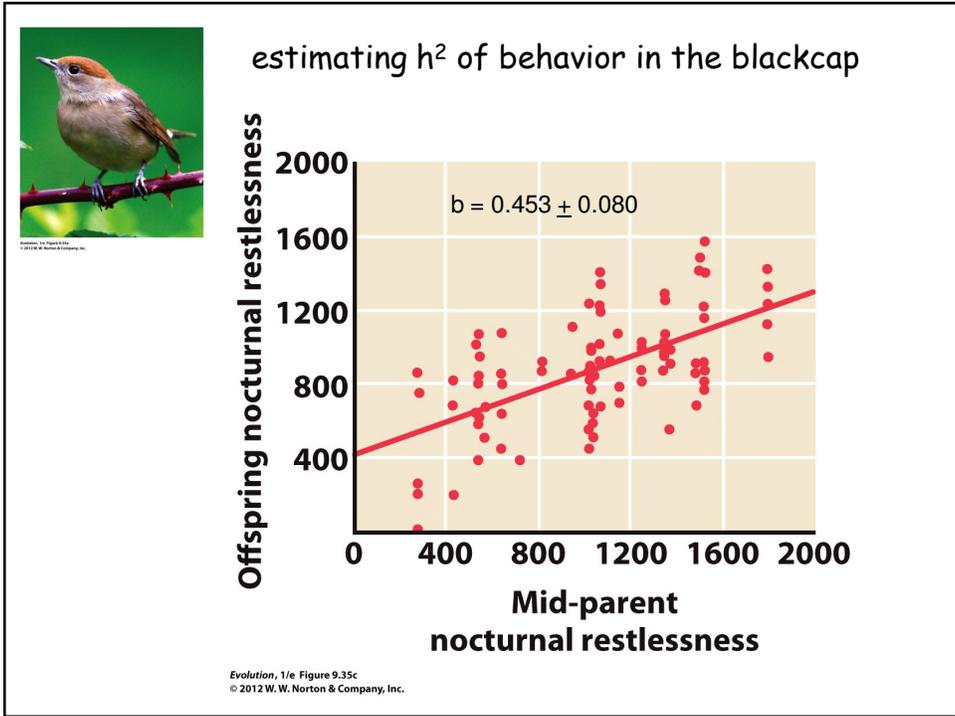
when offspring resemble parents their phenotypes covary



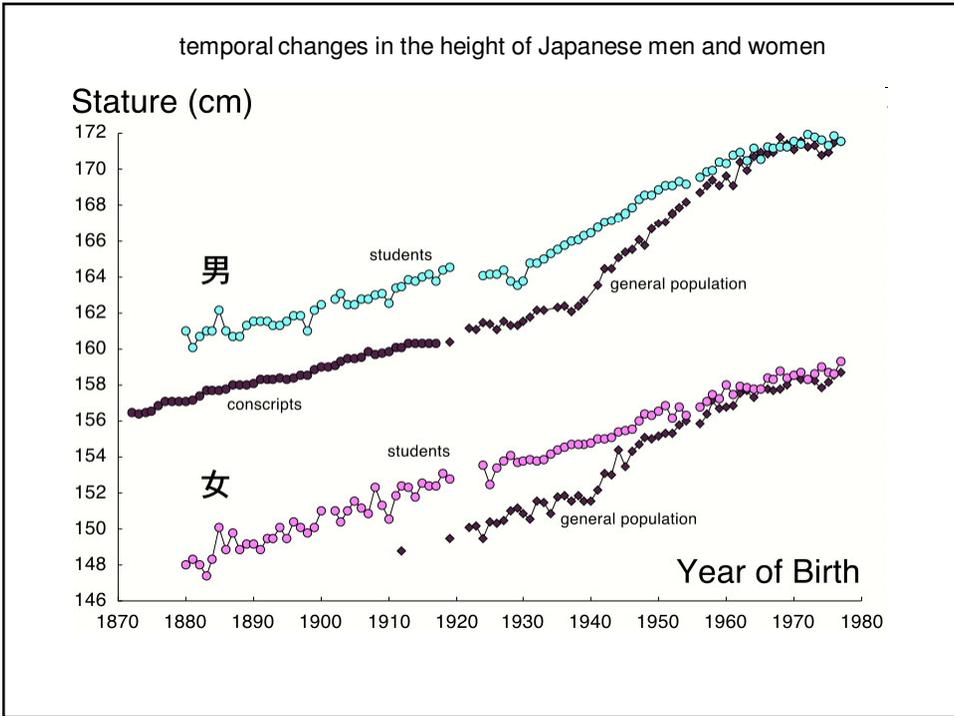
Regression: want to predict **y** from **x**  
 We produce a regression coefficient or slope for a line  
 The line goes through the mean **x** and mean **y**

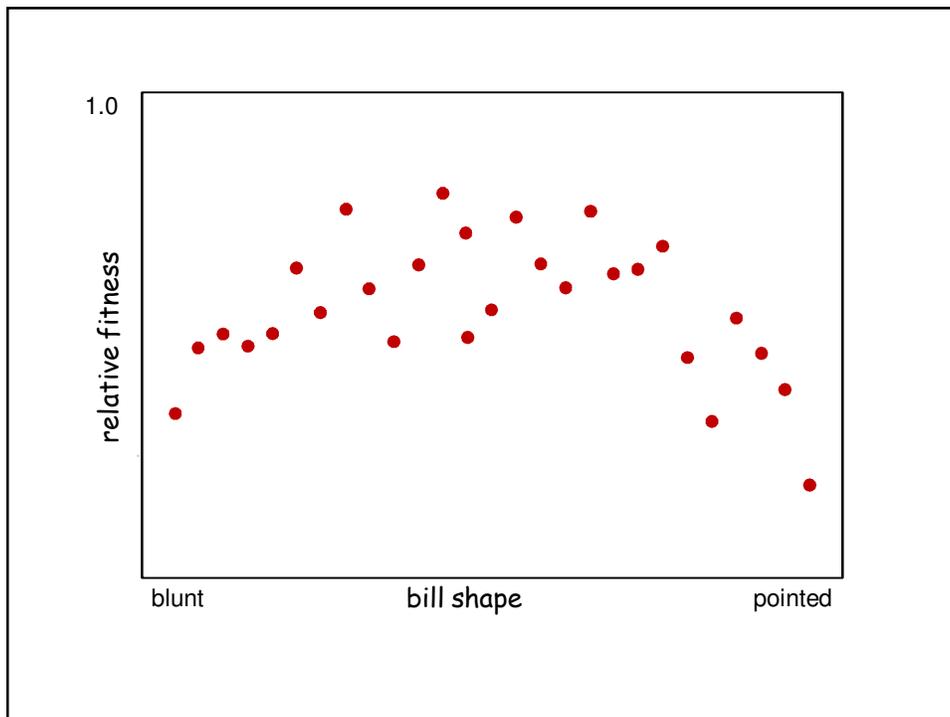
$$\text{Regression coefficient} = \frac{Cov(x, y)}{Var(x)} = \frac{\frac{1}{2}V_A}{V_P} = \frac{1}{2}h^2$$





### measuring selection on quantitative traits





the fitness ( $w$ ) of a trait ( $z$ ) can be estimated as:

$$w = \alpha + \beta z + (\gamma/2)z^2$$

$\alpha$  is the y-intercept of the fitness function

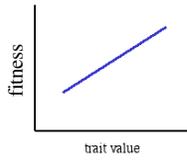
$\beta$  is the fitness function's slope

$\gamma$  measures the amount of curvature in the fitness function

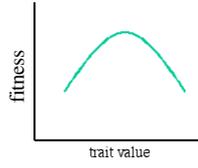
$\beta$  and  $\gamma$  are the selection gradients

patterns of selection on quantitative traits

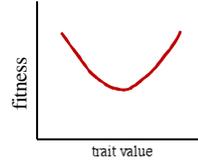
directional



stabilizing

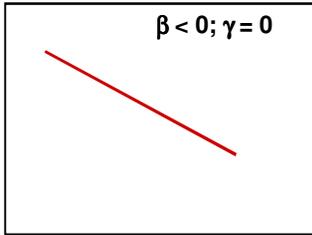


disruptive

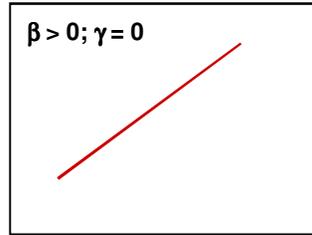


relative fitness

$\beta < 0; \gamma = 0$

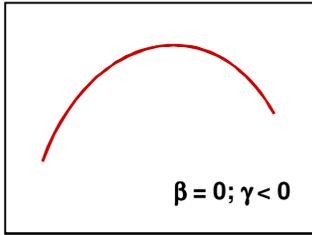


$\beta > 0; \gamma = 0$

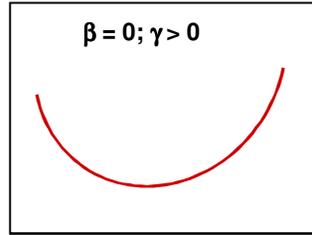


relative fitness

$\beta = 0; \gamma < 0$

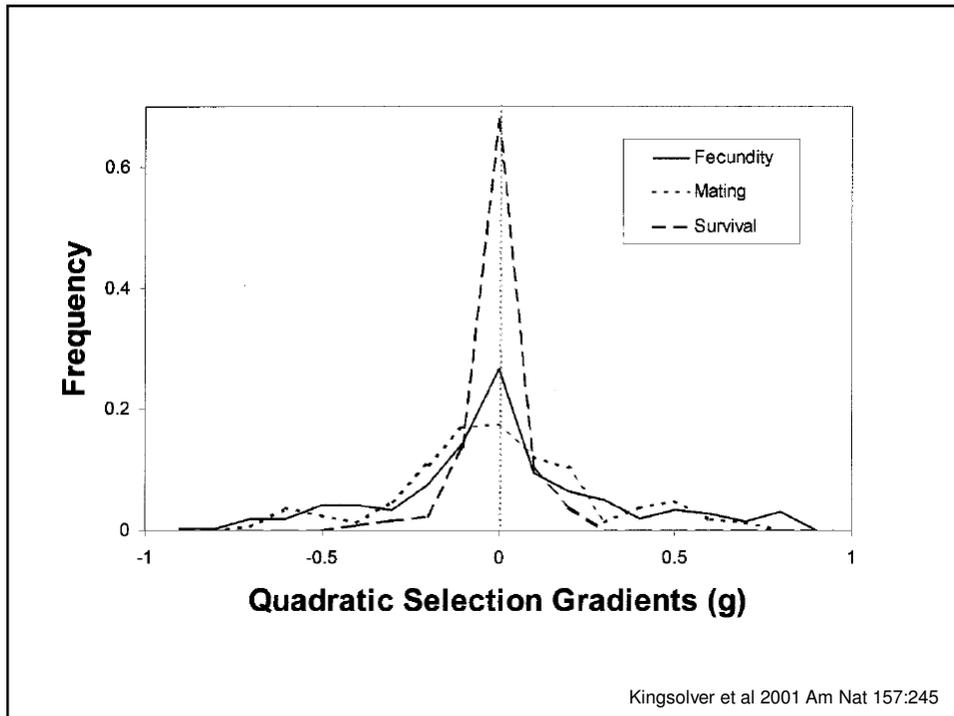
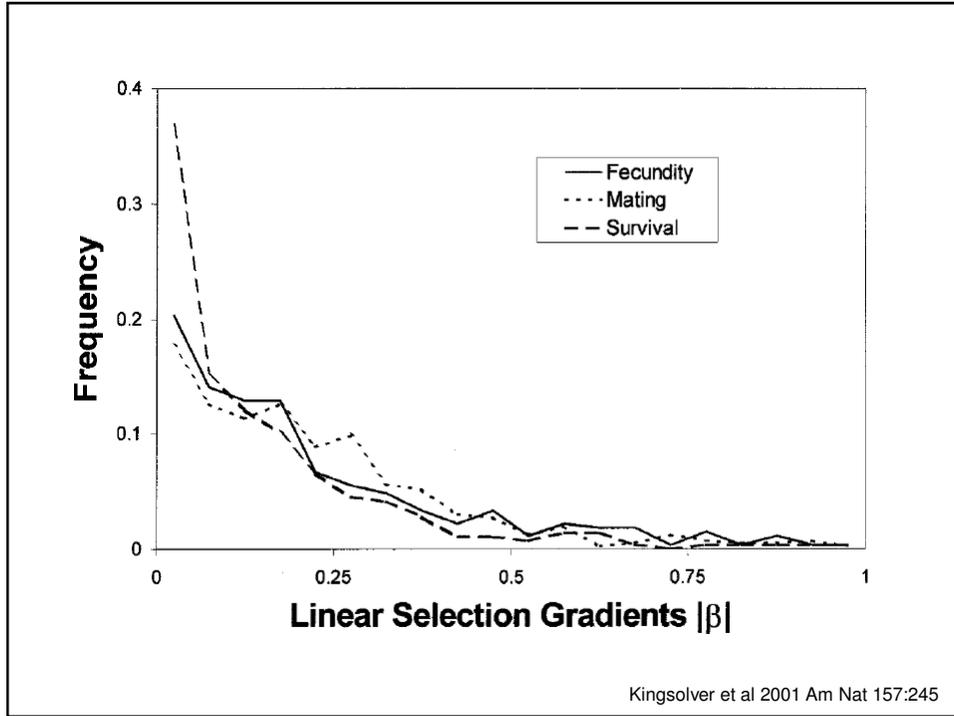


$\beta = 0; \gamma > 0$



phenotype value

phenotype value



### Evolution of quantitative characters

phenotypic variance in a trait can be partitioned into several genetic variance components

additive genetic variance ( $V_A$ ) represents the heritable component of the phenotype

selection will change the genetic variation in a quantitative trait in a manner similar to one with simpler genetics

heritability can be estimated from breeding studies

heritability is a property of a population