

# Lecture 3, Part I: Anisotropic flow



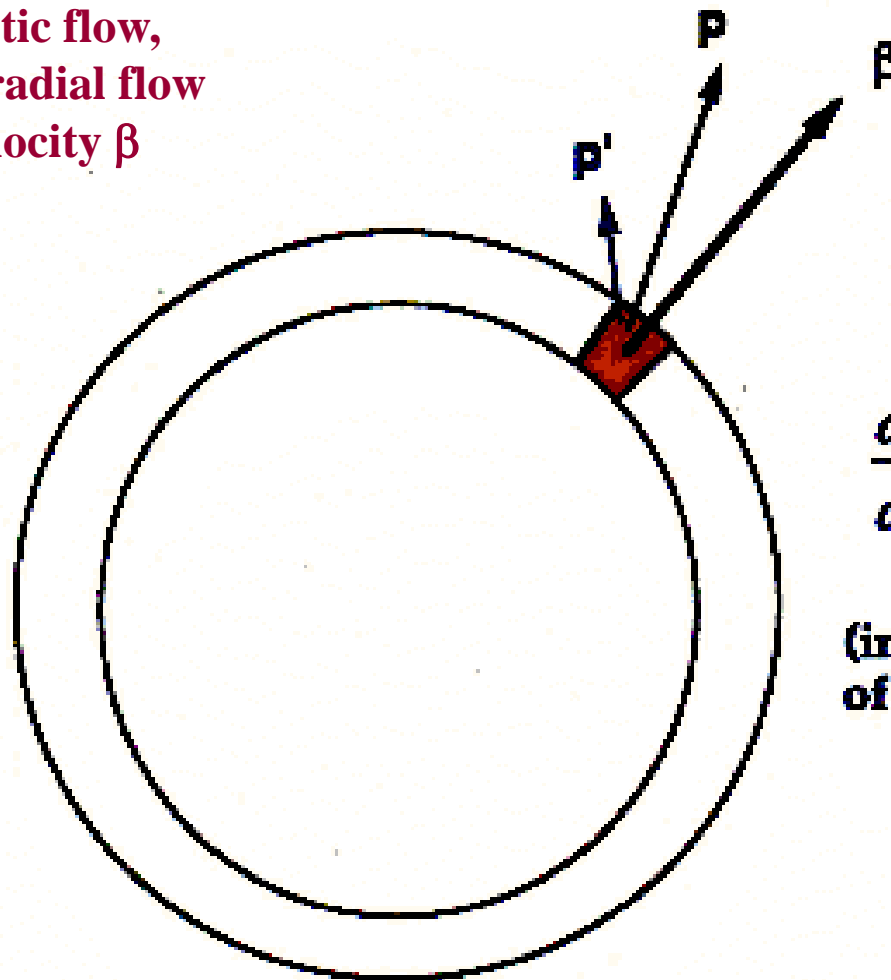
# Emission from a Thermal Expanding Source

No elliptic flow,  
strong radial flow  
with velocity  $\beta$

Central  
collisions

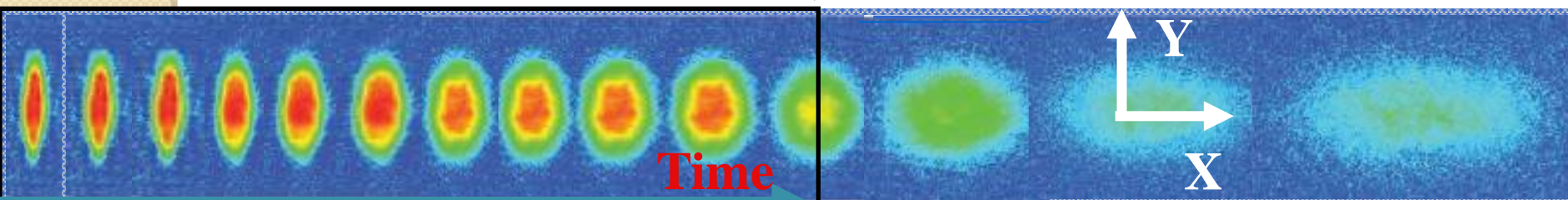
Reaction  
plane

Dashed li  
sphere ra

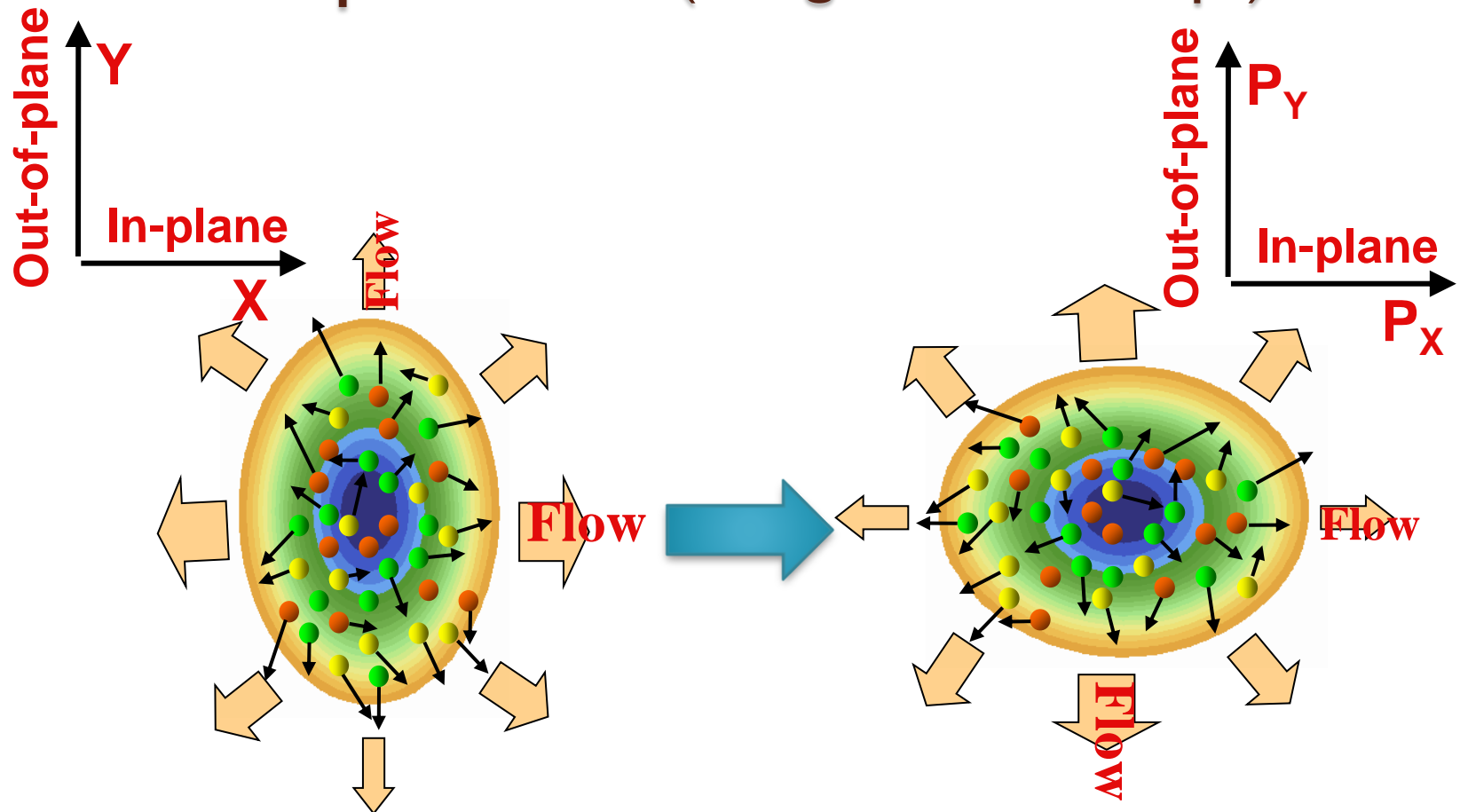


$$\frac{d^3 N}{dp'^3} \approx e^{-E/T}$$

(in the rest frame  
of each element)

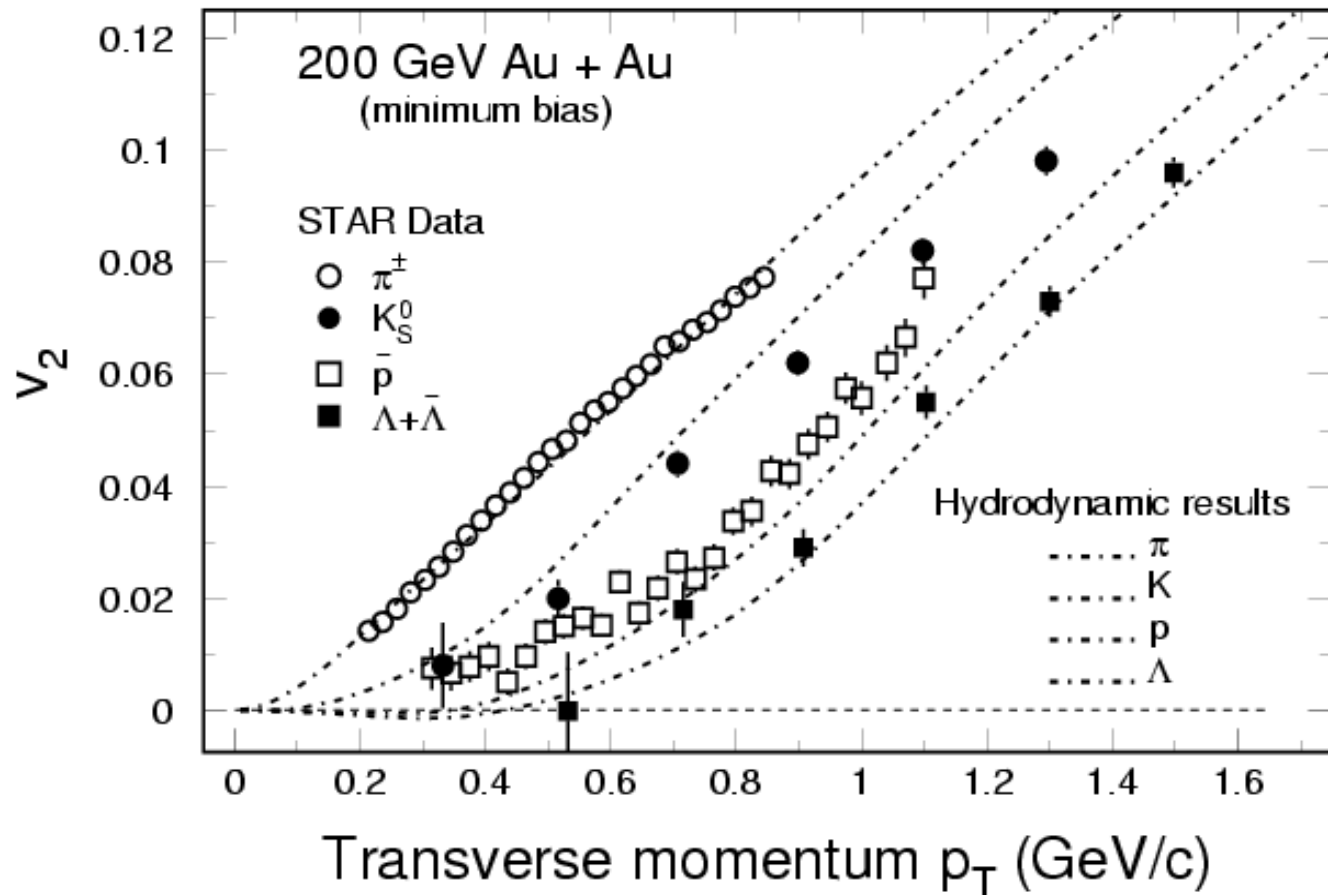


# Elliptic Flow (the general concept)



- If no interactions (collectivity) between partons (hadrons), then particles will be emitted isotropically in momentum space.
- If interactions, then  $p_x > p_y$ . Anisotropy ( $v_2$ ) is measure of interaction strength.

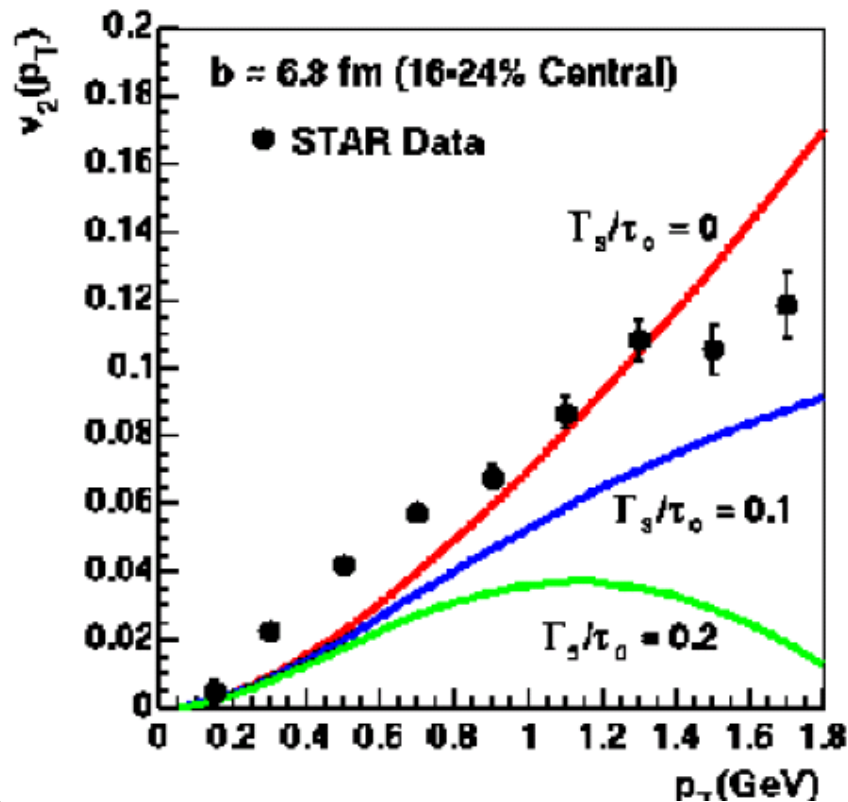
# Elliptic flow described by fluid dynamics



Consequence: if ideal hydrodynamics works (= zero mean free path) then the interaction strength between partons is maximum = strong coupling = ideal fluid behavior

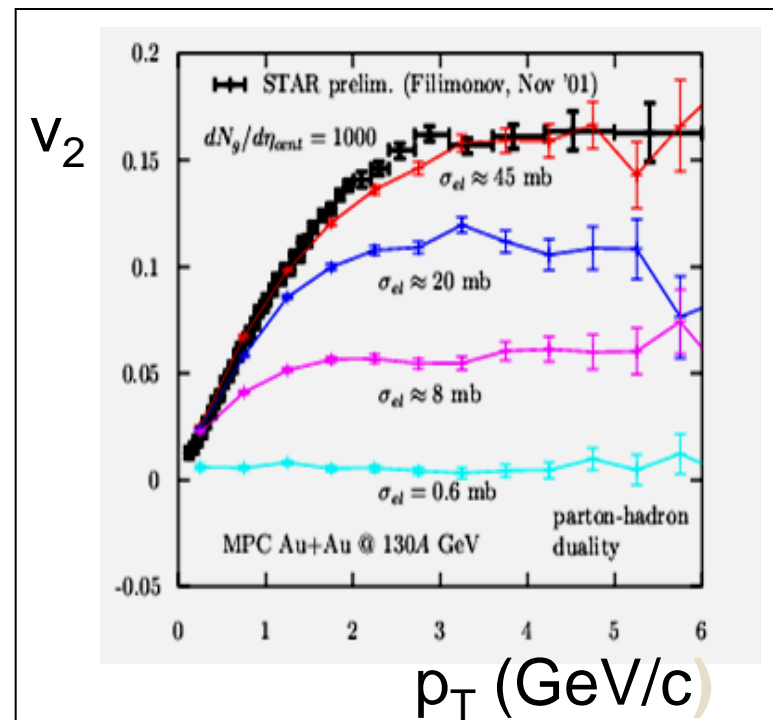
# How strong is the coupling ?

Navier-Stokes type calculation  
of viscosity – near perfect liquid  
Viscous force  $\sim 0$



R. BELLWIED

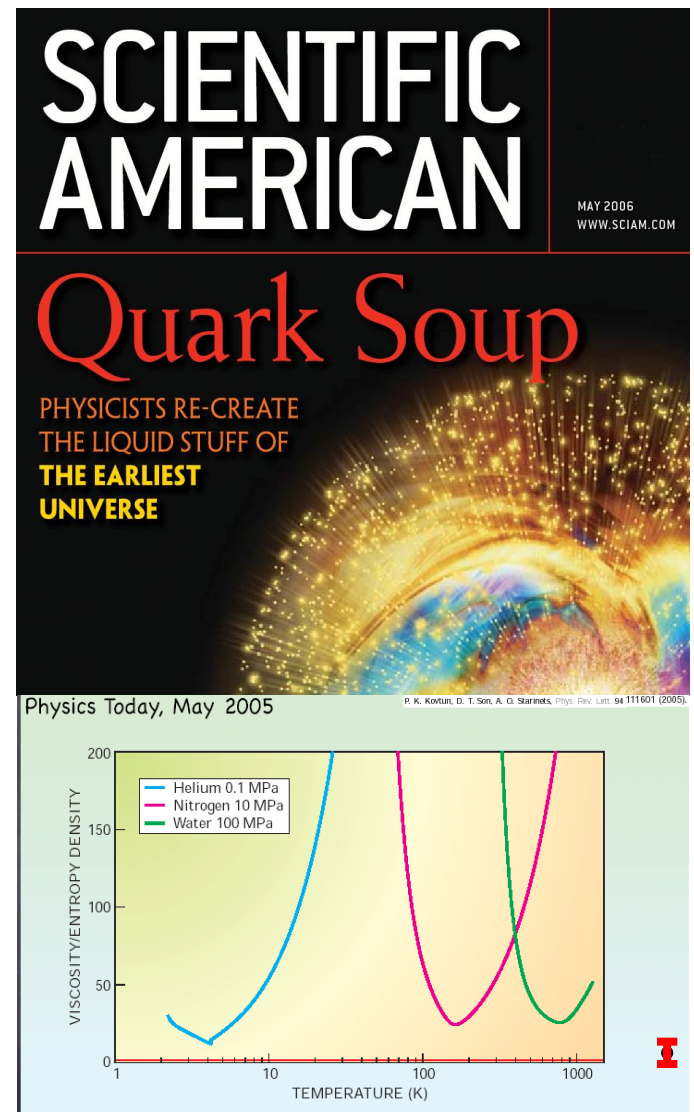
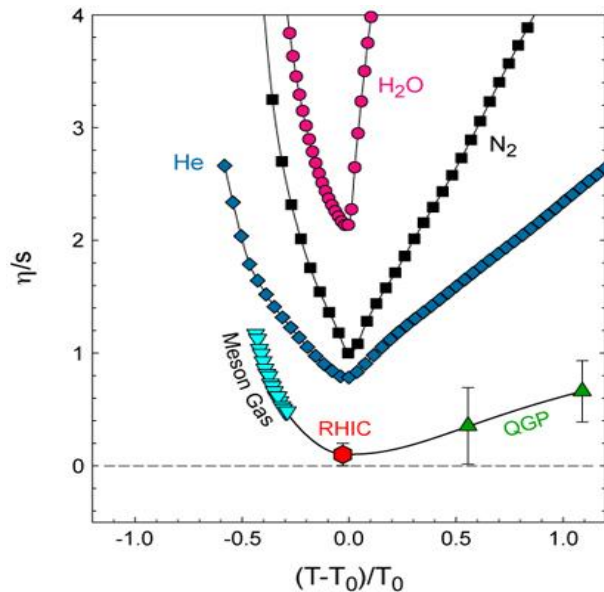
Simple pQCD processes do not  
generate sufficient interaction  
strength (2 to 2 process = 3 mb)



Recently revised through enhanced  
2 to 3 processes (multi-parton)  
(BAMPS code, Frankfurt)

# Lessons from RHIC: The Quark Soup (AIP Science Story of 2006)

Lacey et. al, PRL.98:092301,2007

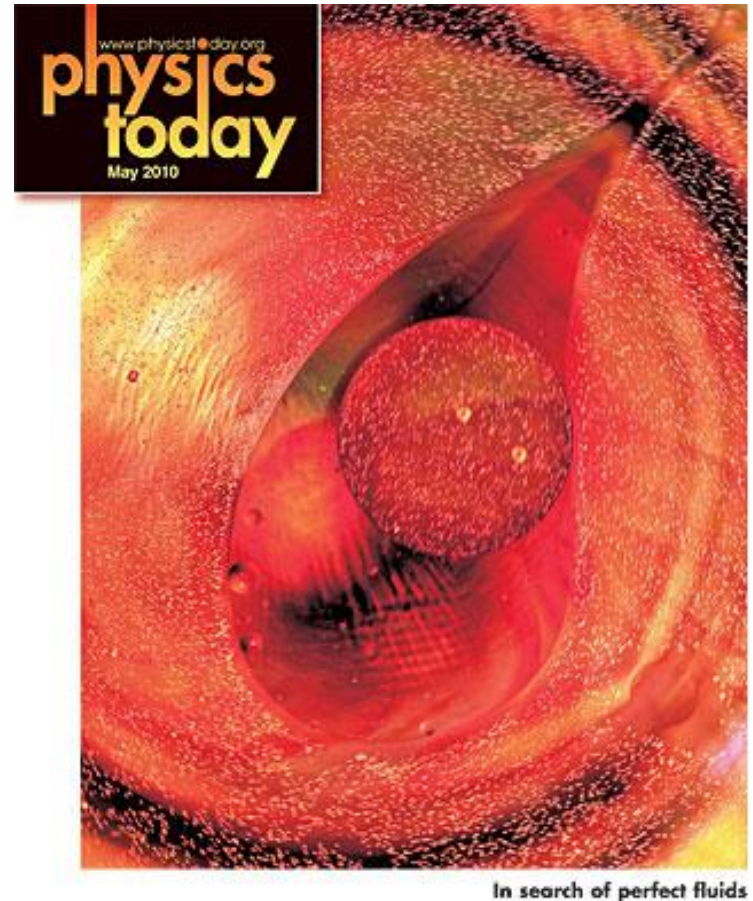
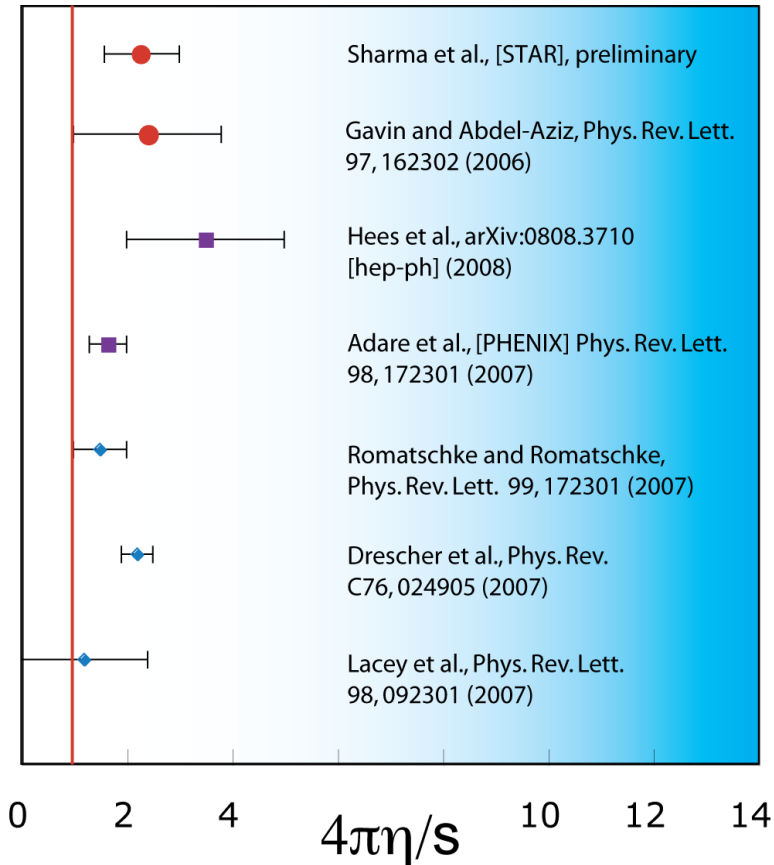


The early universe behaves like a near perfect liquid, not like a gas or plasma. 400 times less viscous than water, 10 times less viscous than superfluid helium !

R. BELLWIED

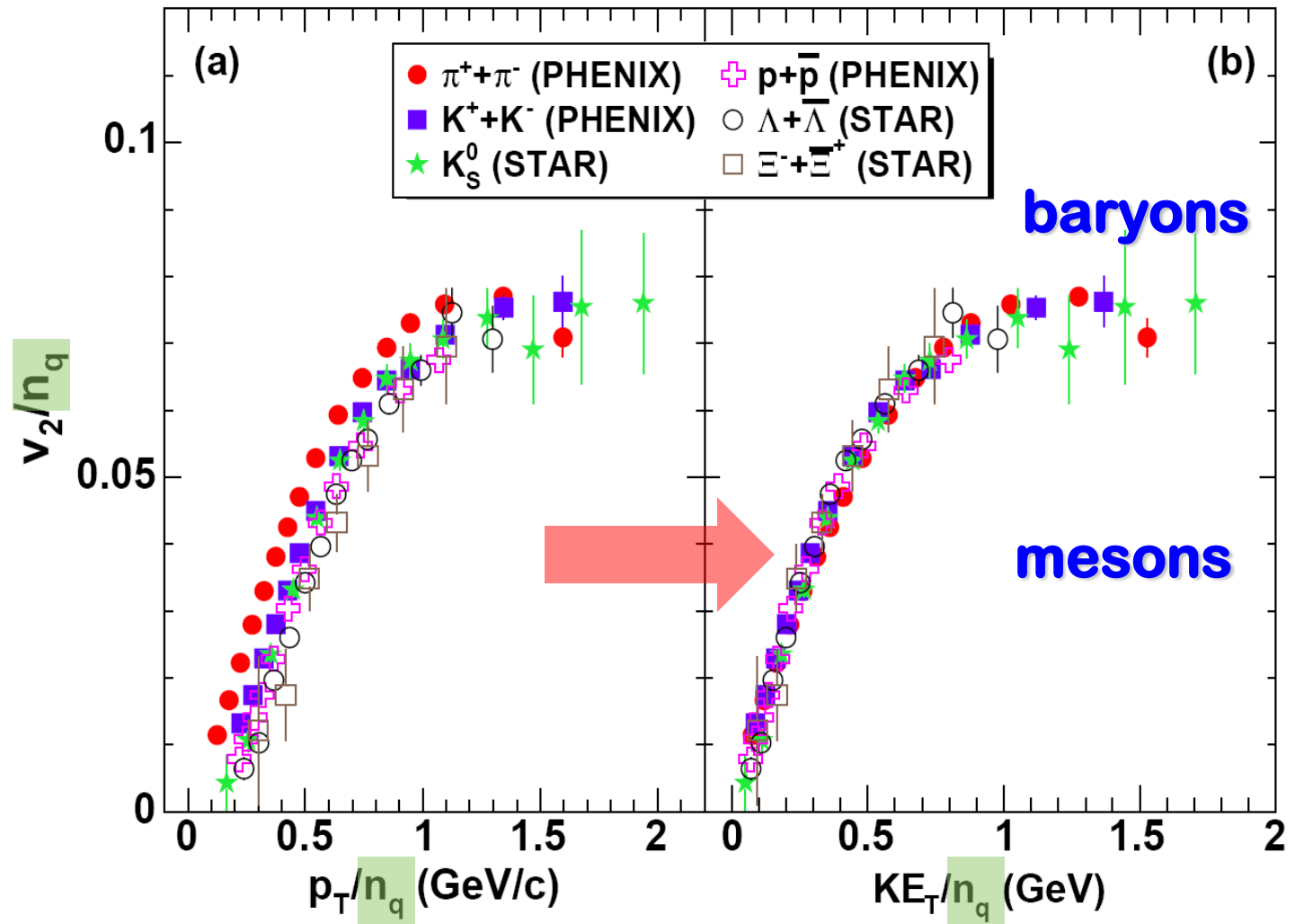


# Experimental Verification



Collective flow confirms the strong coupling nature of the deconfined matter produced at RHIC and the LHC

# How can light quark observables contribute ?

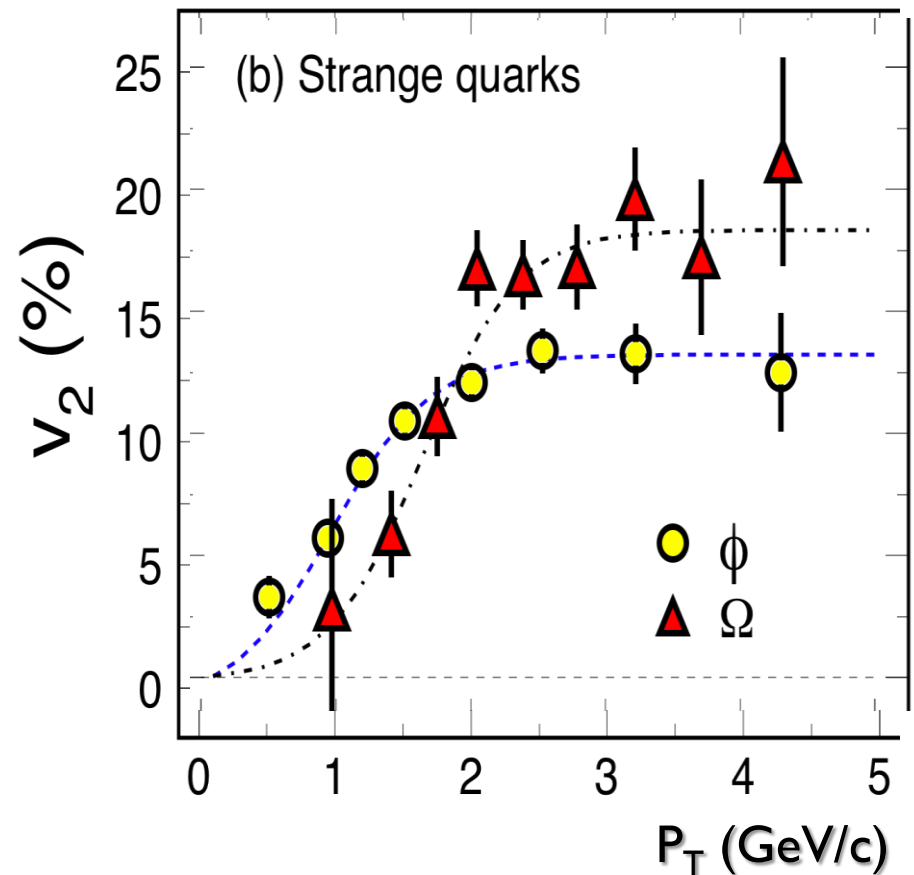
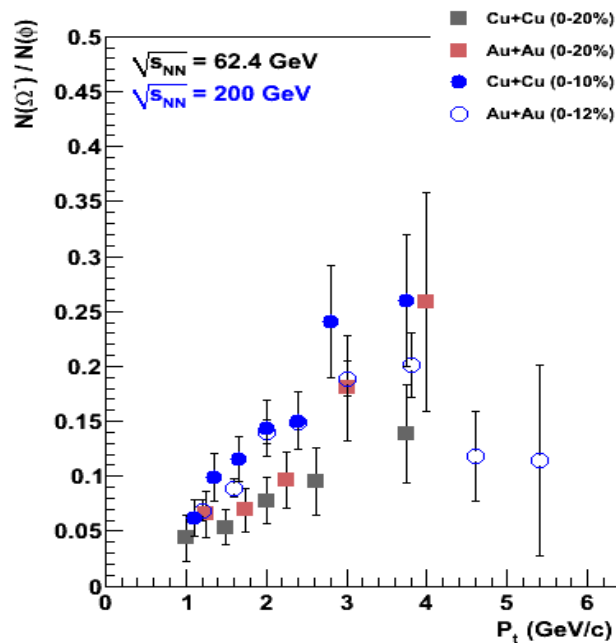


at low  $p_T$ : mass scaling (hadronic nature)  
 at mid  $p_T$ : quark scaling (partonic nature)



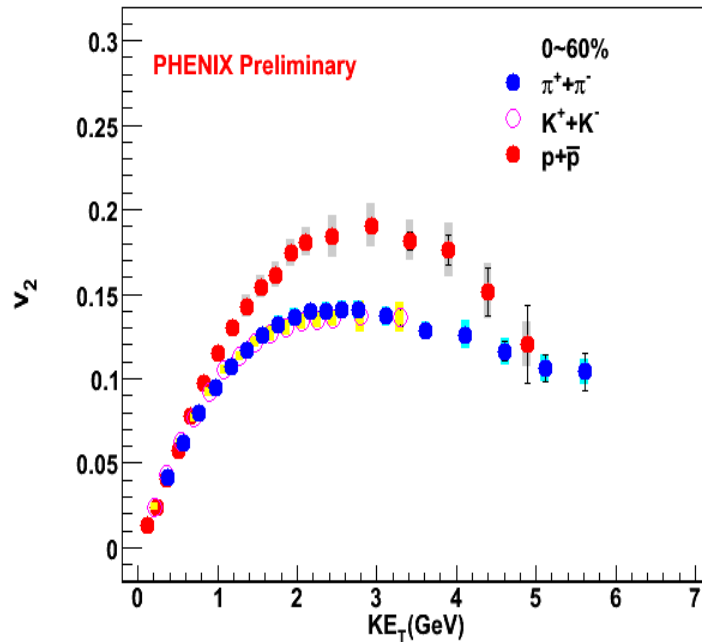
# Confirmed by strange quark ( $\Omega/\phi$ ) measurements

a consistent picture of deconfinement, partonic collectivity, partonic thermalization, and partonic coalescence

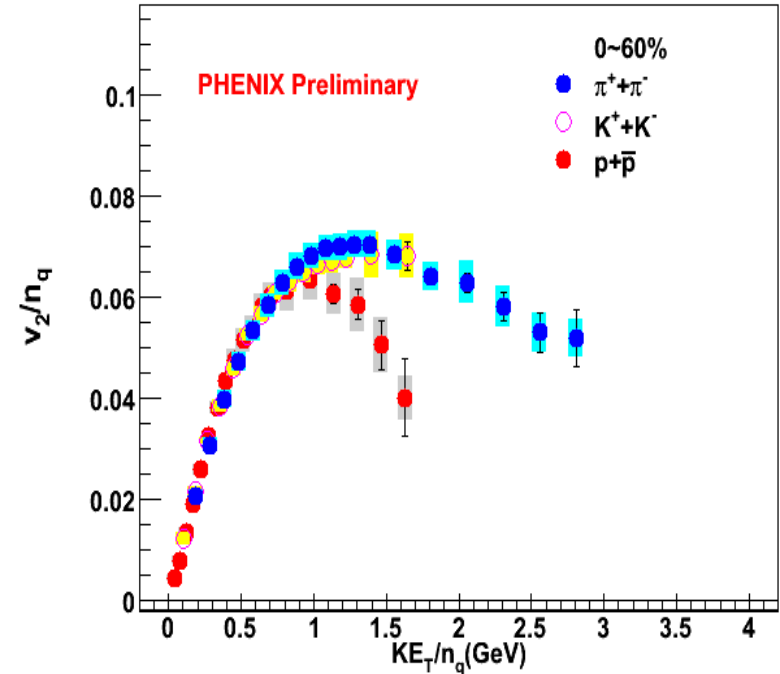


# Breakdown of NCQ scaling

Transverse kinetic energy:  $KE_T \approx m_T - m$ , where  $m_T^2 = p_T^2 + m^2$



$KE_T$  scaling works for baryons and mesons separately at moderate  $p_T$



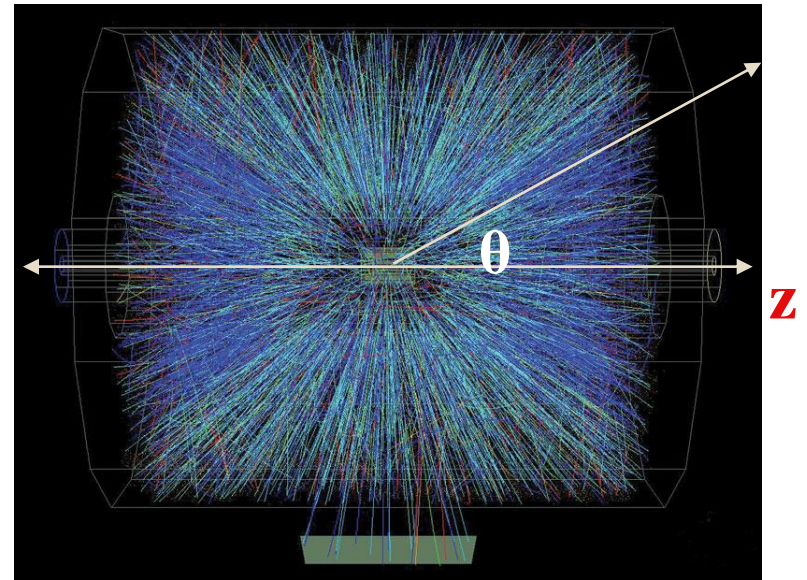
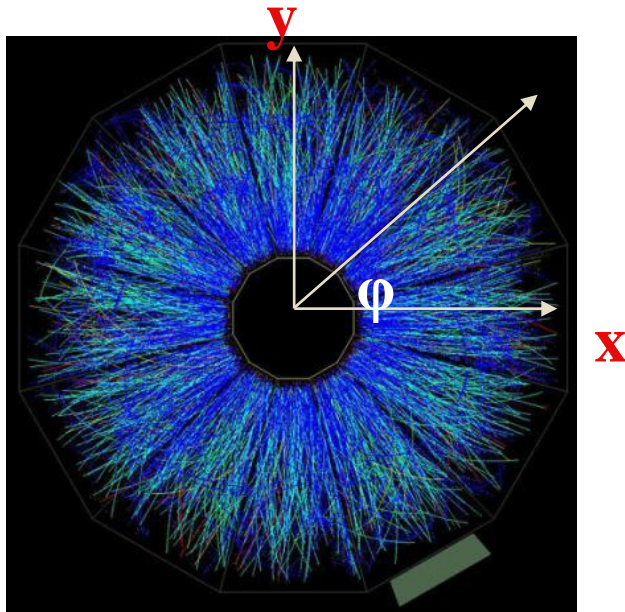
At low  $p_T$   $KE_T/n_q$  scaling suggests flow established at partonic level; breaks down at  $KE_T/n_q > 1$  GeV

# L3, Part I: Fluctuations /Correlations



# Definition of angular variables

- Momentum, azimuthal angle and pseudo-rapidity of the emitted particles are used to study the collision



- $\varphi$  is the azimuthal angle and  $\eta$  is the pseudo-rapidity defined as:

$$\eta = -\ln \left( \tan \left( \frac{\theta}{2} \right) \right)$$

- A correlation study of the angular difference variables  $\Delta\eta$  and  $\Delta\varphi$  of the emitted particles.

# Correlation Measure (Pearson's coefficient)

- $\rho$  = Two particle density
- Sibling Pairs

$$\rho_{sib}(p_t, \eta, \phi) = \frac{\overline{n_a n_b}}{Area}$$

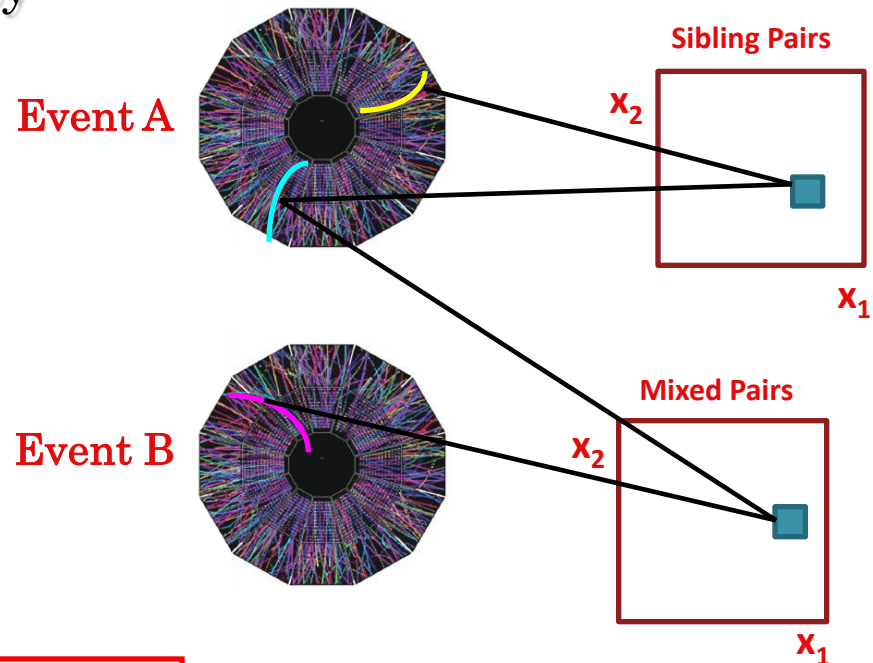
- Mixed Pairs

$$\rho_{ref}(p_t, \eta, \phi) = \frac{\overline{n_a n_b}}{Area}$$

- Final Measure:

$$\frac{\rho_{sib} - \rho_{ref}}{\sqrt{\rho_{ref}}} = \frac{\Delta\rho}{\sqrt{\rho_{ref}}} \rightarrow \sqrt{\rho_{ref}} \frac{\Delta\rho}{\rho_{ref}}$$

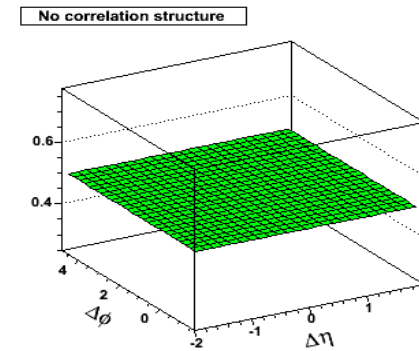
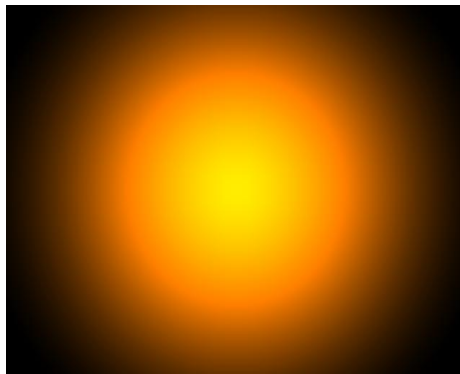
Normalized Ref Pairs:  
Total number of sibling to mixed pairs  
 $\frac{dN_{ch}}{d\eta d\phi}$



- Number of correlated pairs *per* final state particle

# Di-hadron correlations – the original assumptions

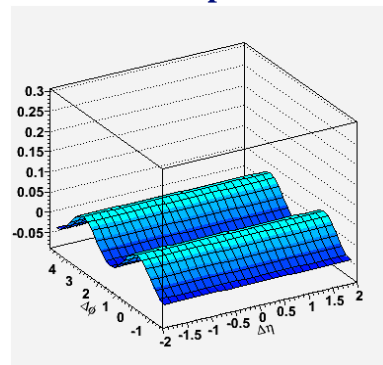
- If a static thermalized system is formed, the emissions would be isotropic



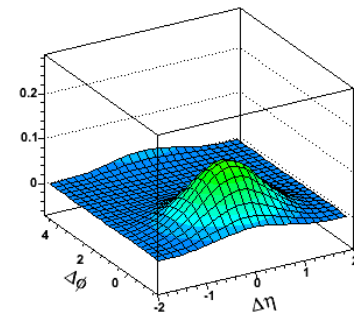
Equal probability for each particle in any direction of emission

- In high energy nuclear and particle physics we expect specific correlation effects
  - Resonance decay
  - Anisotropic flow
  - Jet fragmentation

Anisotropic flow



Jet fragmentation

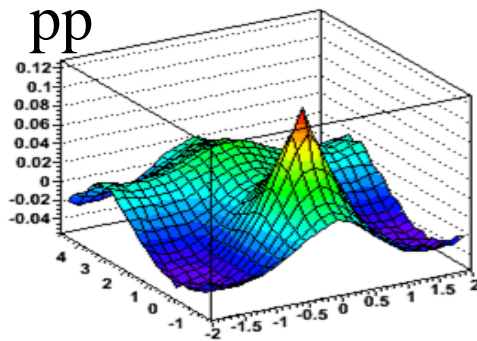




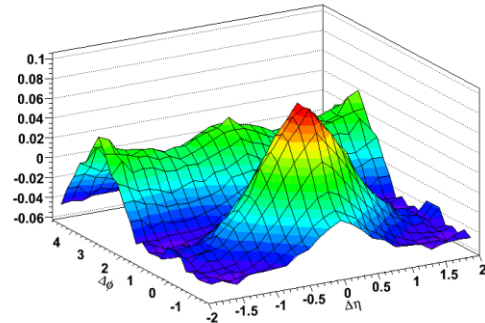
Number correlations  
in coordinate space  
as a f(centrality)

# Lots of structure in RHIC emissions

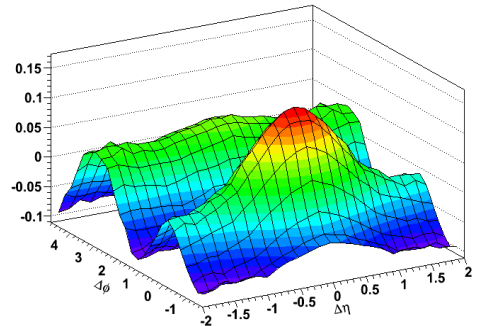
$$\frac{\Delta\rho}{\sqrt{\rho_{ref}}}$$



HBT subtracted: 50 - 60%

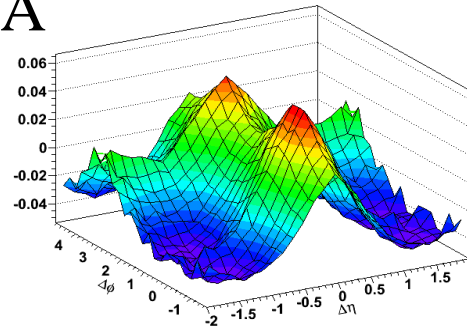


HBT subtracted: 20 - 30%

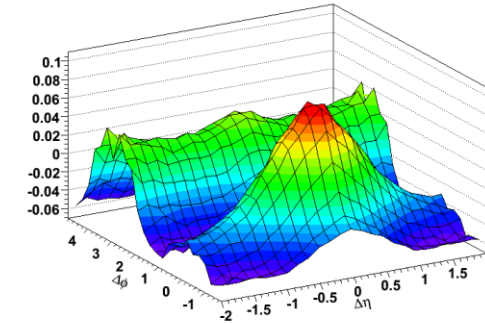


AA

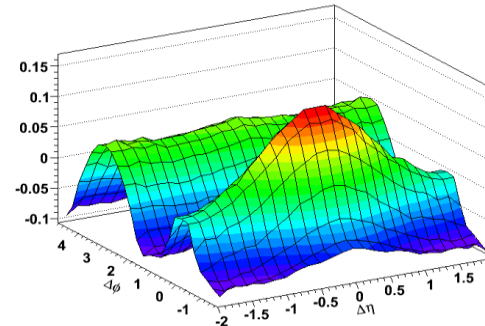
HBT subtracted: 70 - 80%



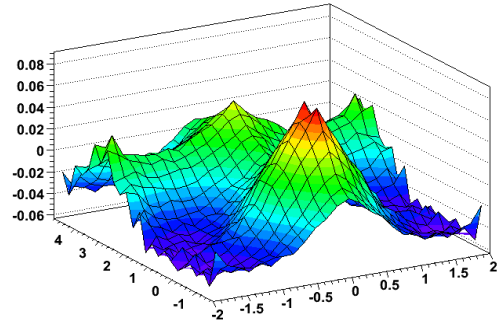
HBT subtracted: 40 - 50%



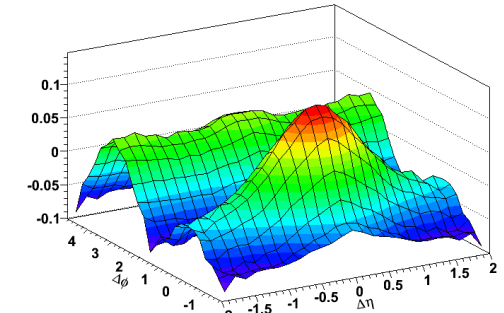
HBT subtracted: 10 - 20%



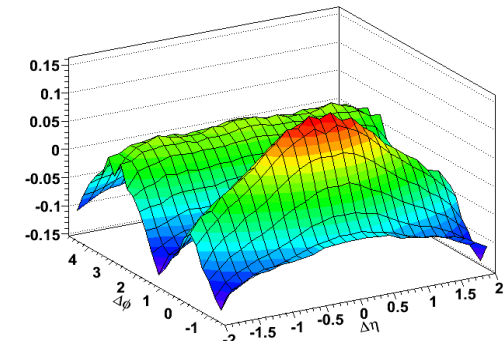
HBT subtracted: 60 - 70%



HBT subtracted: 30 - 40%

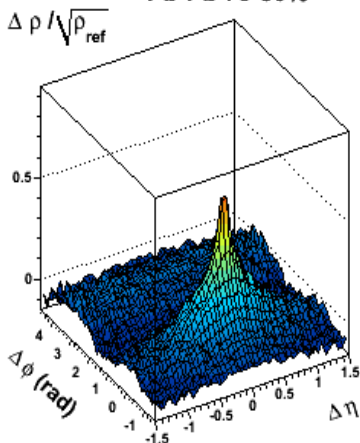


HBT subtracted: 0 - 10%

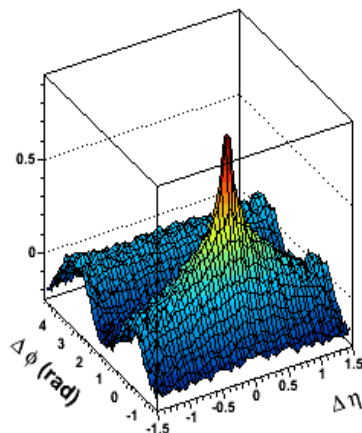


# ...even more pronounced in ALICE

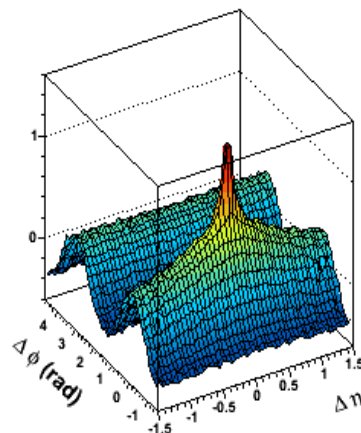
Pb-Pb 70-80%



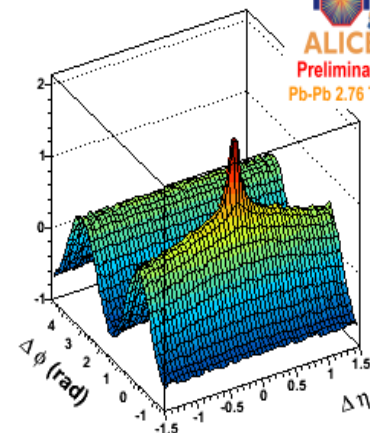
Pb-Pb 60-70%



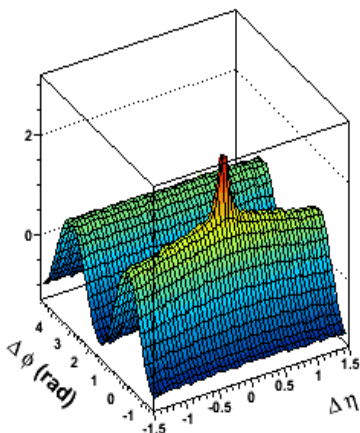
Pb-Pb 50-60%



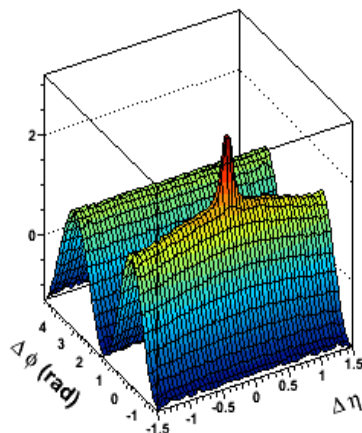
Pb-Pb 40-50%



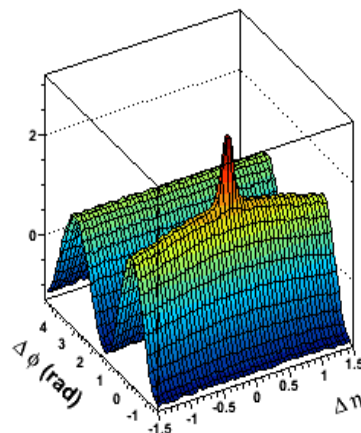
Pb-Pb 30-40%



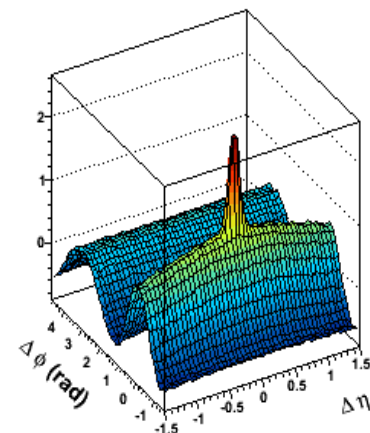
Pb-Pb 20-30%



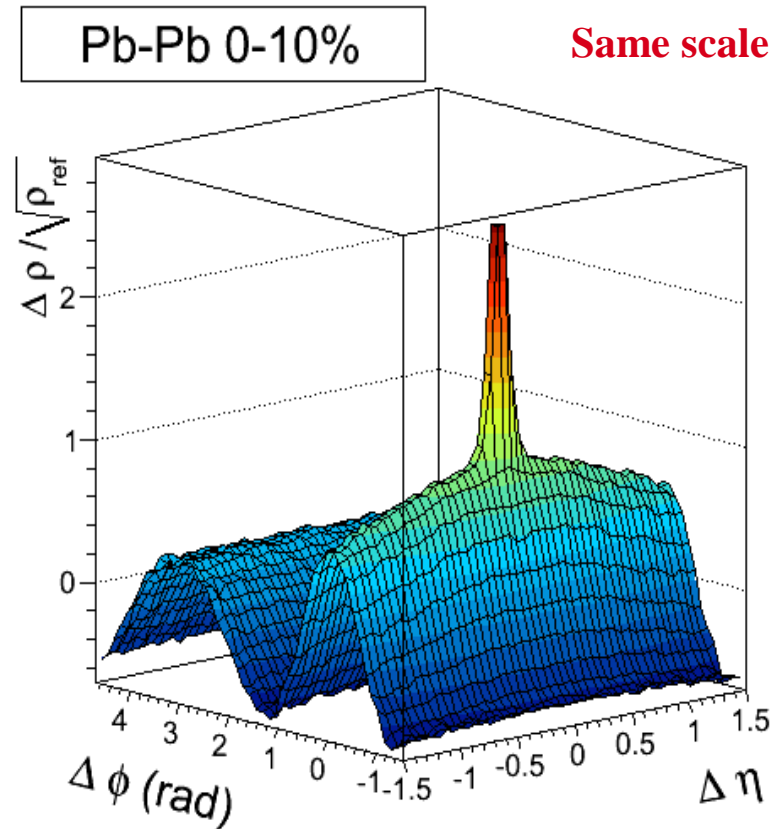
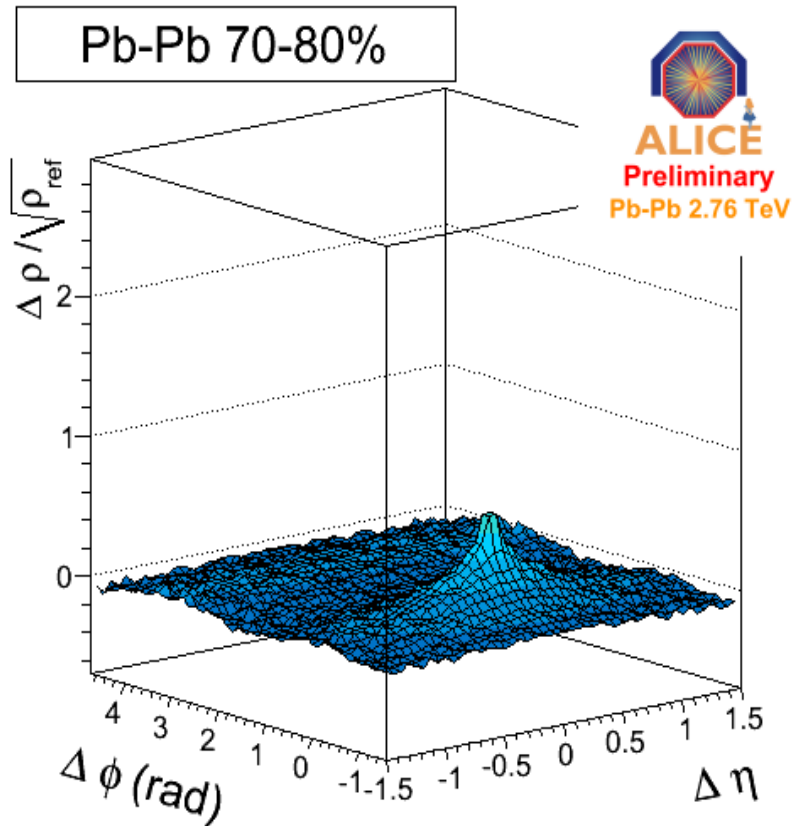
Pb-Pb 10-20%



Pb-Pb 0-10%



# On the same scale from peripheral to central



# Investigation of Fluctuating Initial Conditions

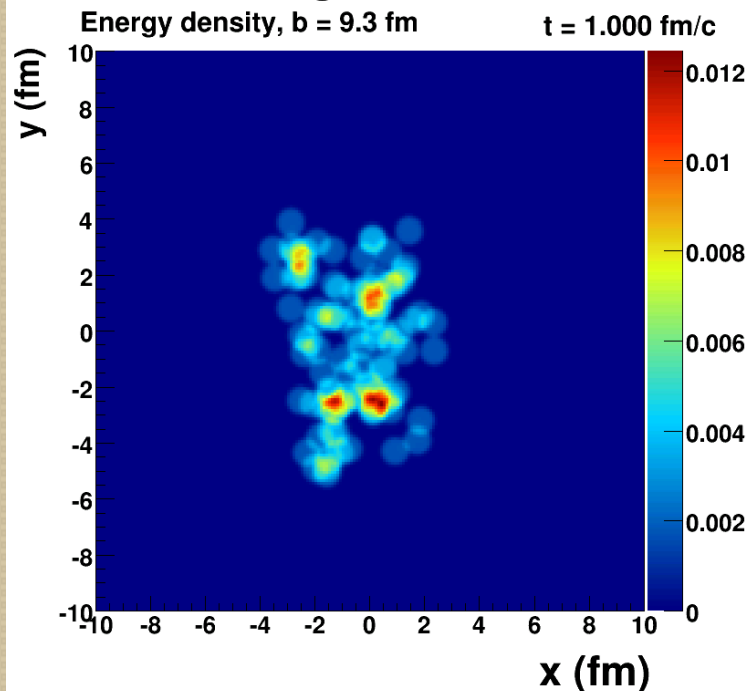
What if the initial energy density fluctuates and is not smooth  
(i.e. the nuclei cannot be described by hard spheres).

Viscous hydro code from M. Luzum and P. Romatschke

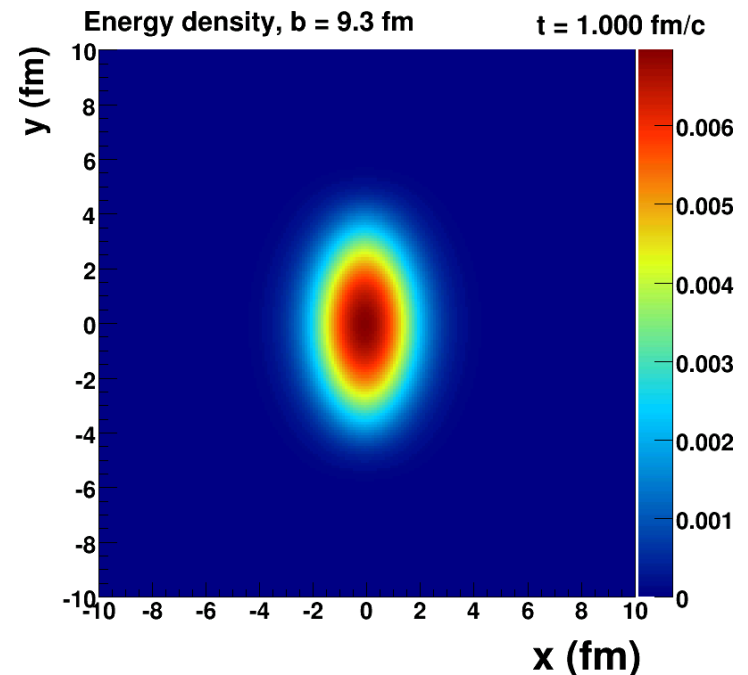
(<http://hep.itp.tuwien.ac.at/~paulrom/codedown.html>)(0900I.488v1)

Settings: 200x200 grid,  $\eta/s = 0.08$

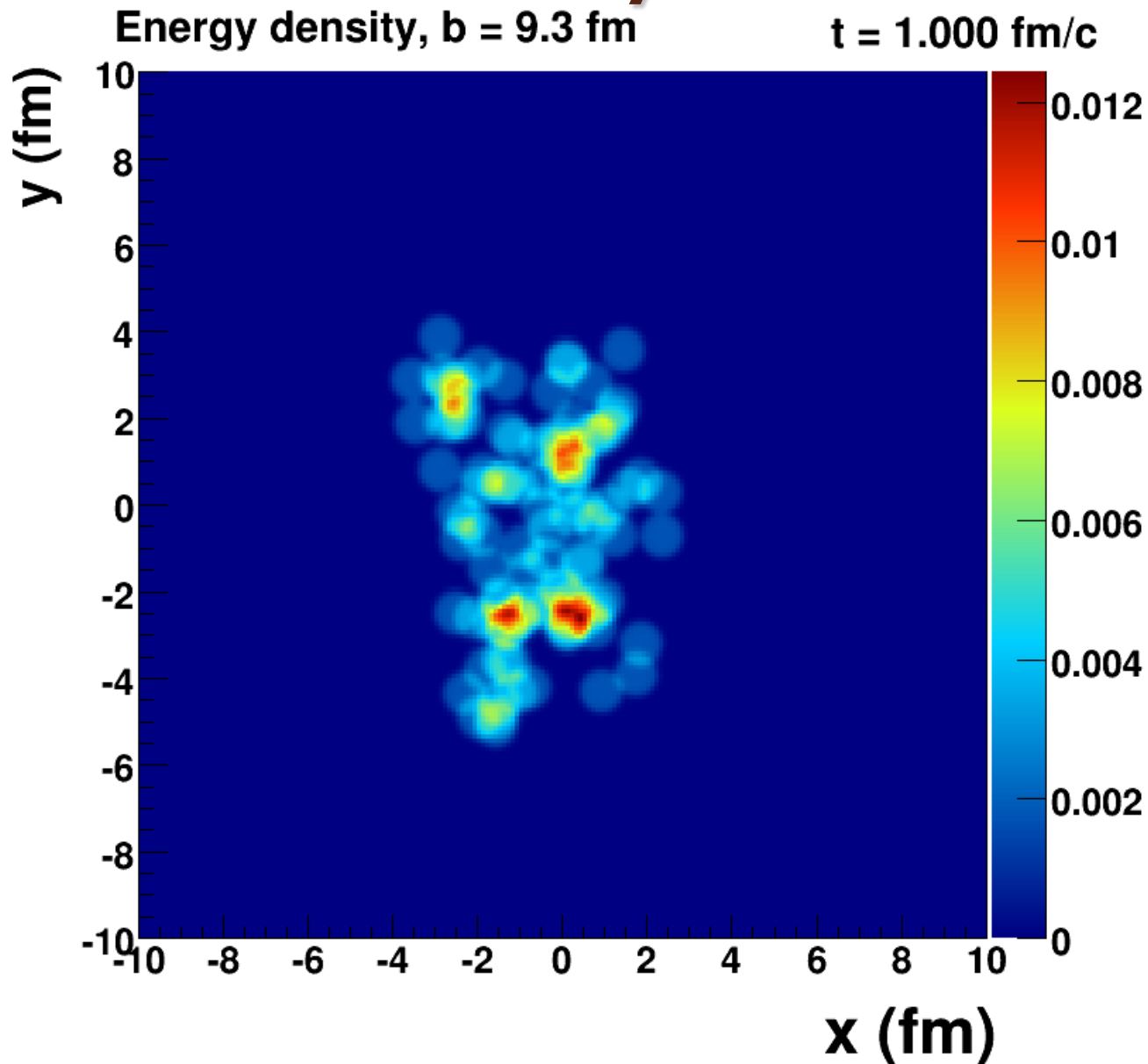
a single event



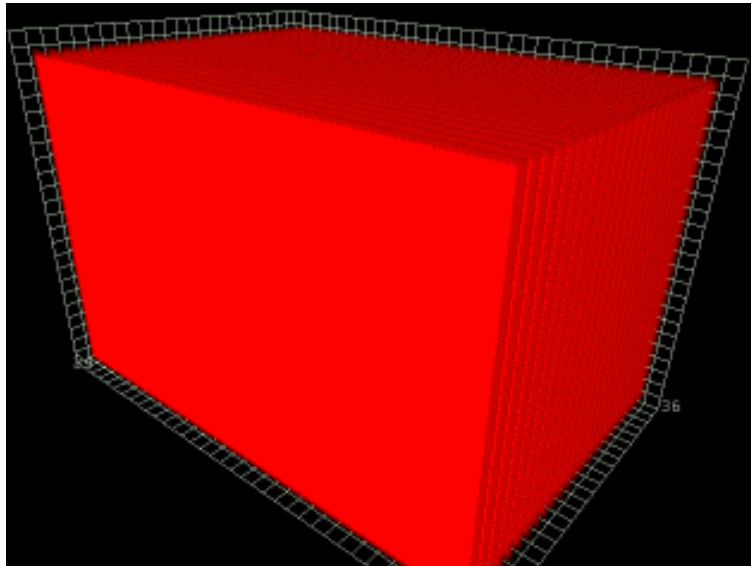
average over 1M Events



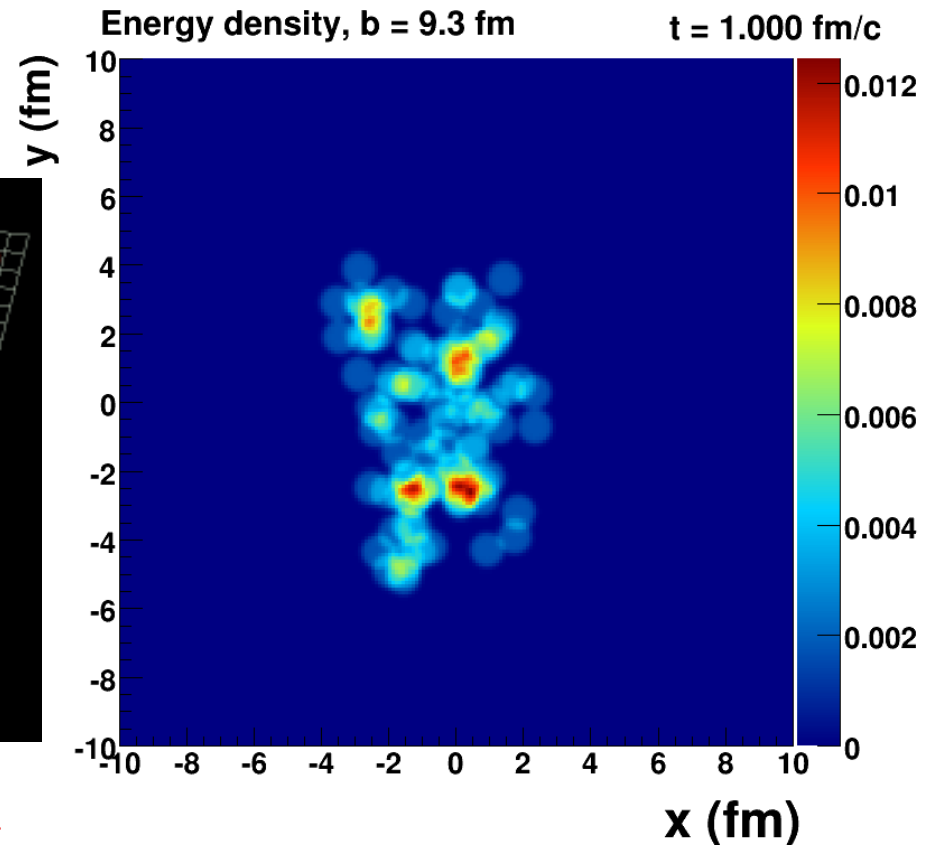
# Time evolution of initial conditions in hydro



# The cooling of the hot QCD vacuum and the hot QCD medium



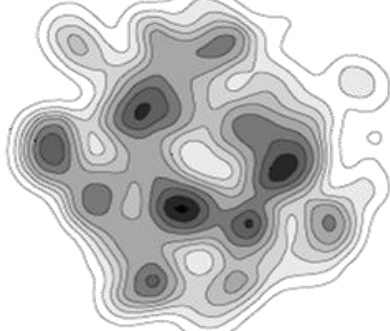
**Lattice QCD calculation  
Adelaide Group**





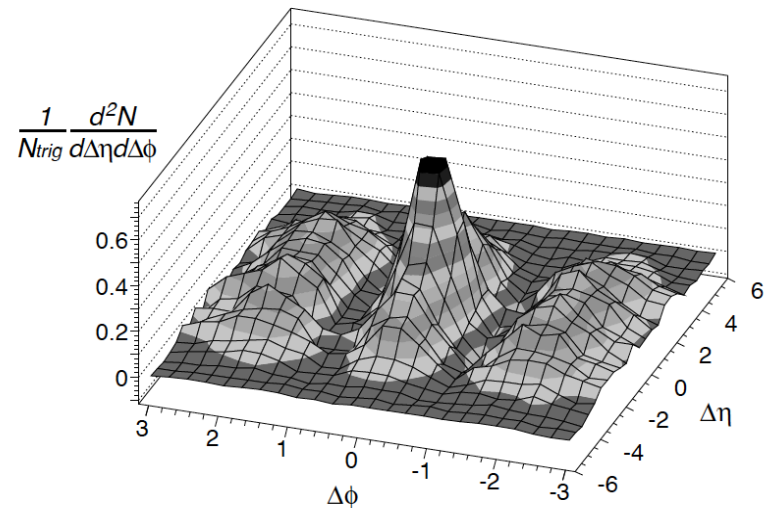
# Initial conditions plus radial expansion

Hama, Grassi, Kodama,  
Takahashi et. al.

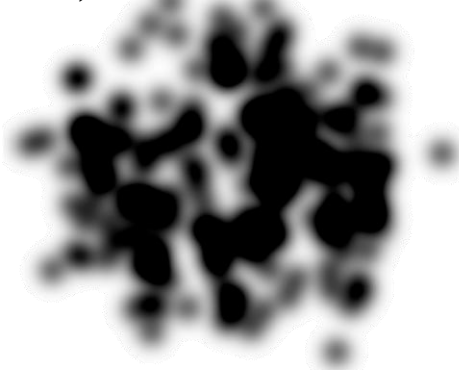


**NexSPheRio**

(color ropes due to nuclear density profile)

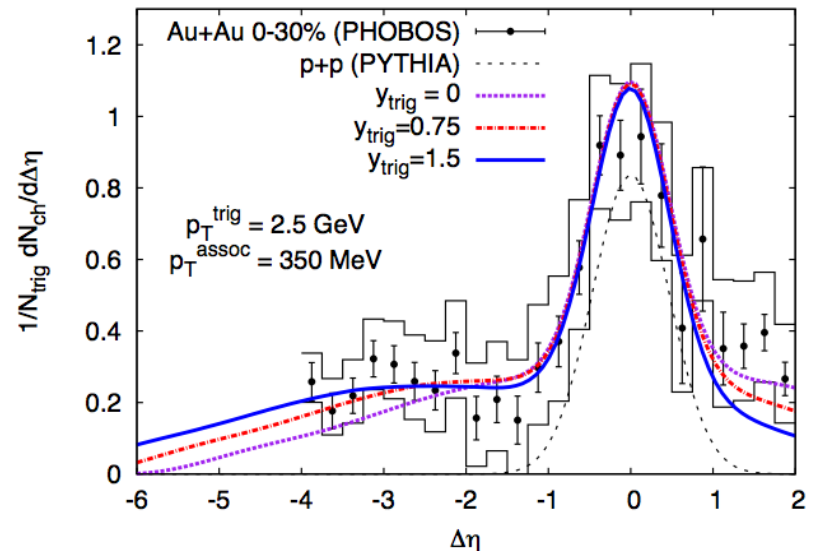


Dumitru, Gelis, McLerran,  
Gavin, Moschelli et al.



**CGC & Glasma**

(flux tubes due to initial gluon profile)



# Many different ideas on origin

- **Initial energy density fluctuations**

- Mishra et.al, Phys. Rev. C 77 (064902) 2008
- Takahashi et.al, Phys. Rev. Lett. 103, 242301 (2009)
- Alver and Roland, Phys. Rev. C 81 (2010) 054905
- Werner et al, arXiv:1104.3269v1
- Sorensen et al, arXiv:1101.1925v1

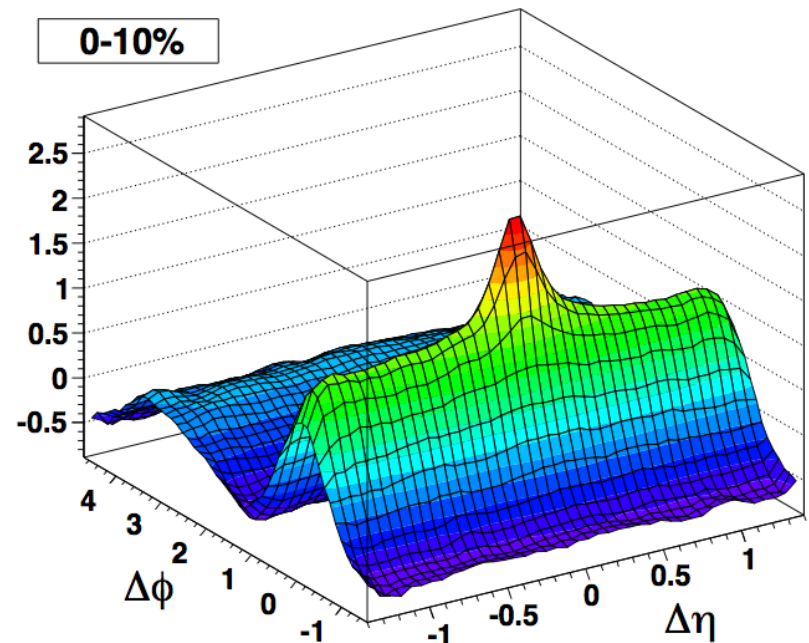
- **CGC flux tubes and/or radial flow**

- Voloshin, Phys. Lett. B 632 (2006) 490
- Dumitru, Gelis, McLerran, Venugopalan Nucl.Phys.A810:91-108,2008
- Gavin, McLerran and Moschelli: Phys. Rev. C79 (2009) 051902
- Moschelli and Gavin: Nucl.Phys.A836:43-58,2010

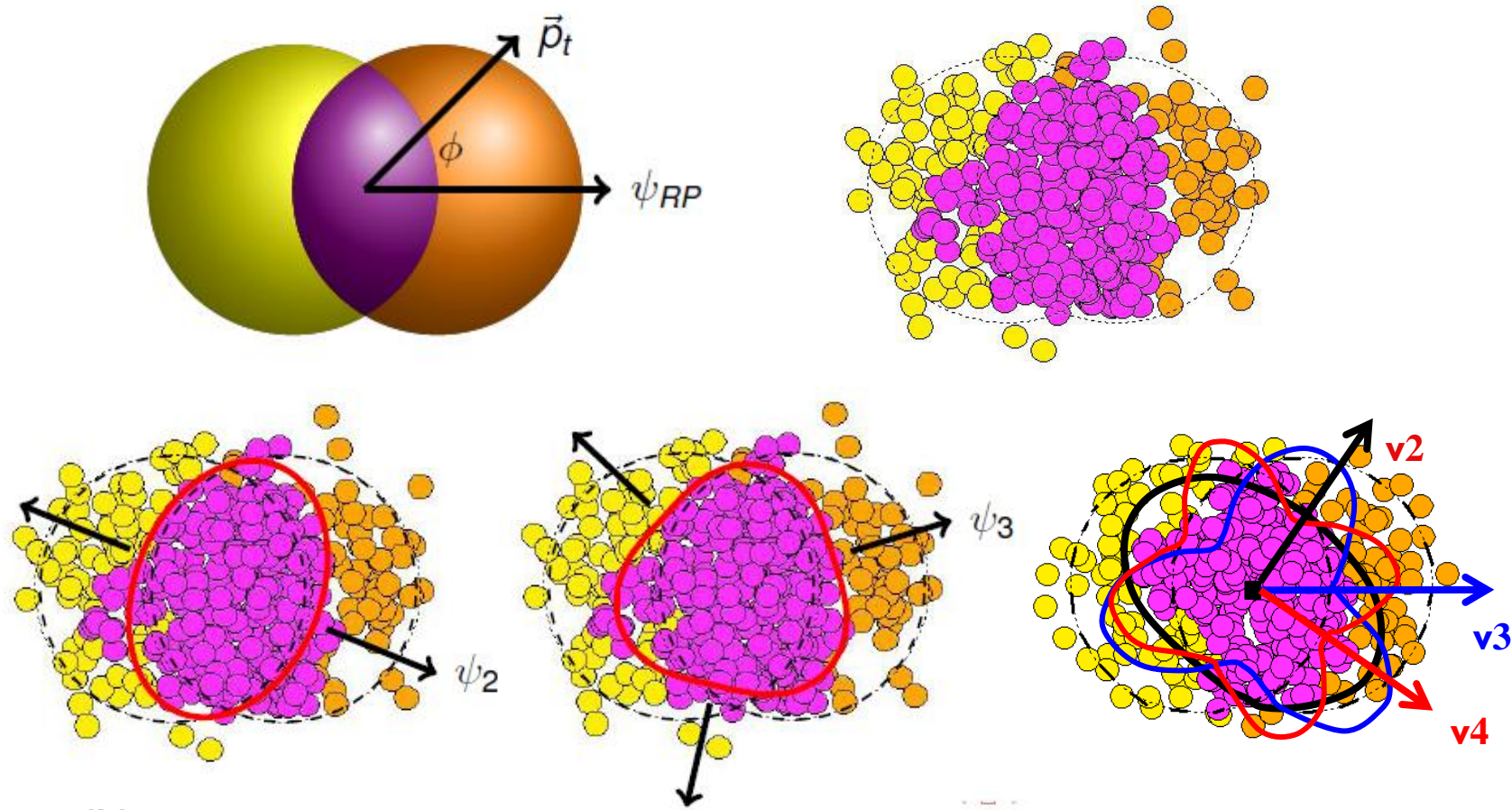
- **Modified mini-jets (pQCD related explanation)**

- T.Trainor, Phys. Rev. C 80 (2009) 044901

**Pb-Pb 2.76 TeV**



# Higher harmonics of initial energy density fluctuations

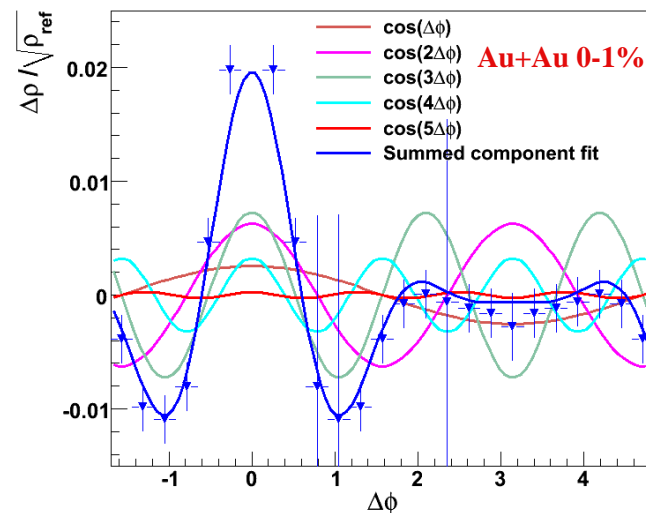
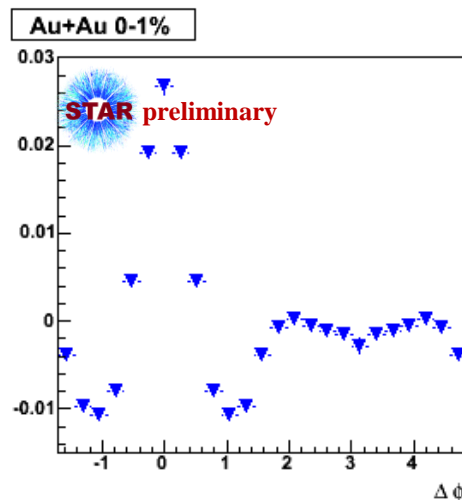
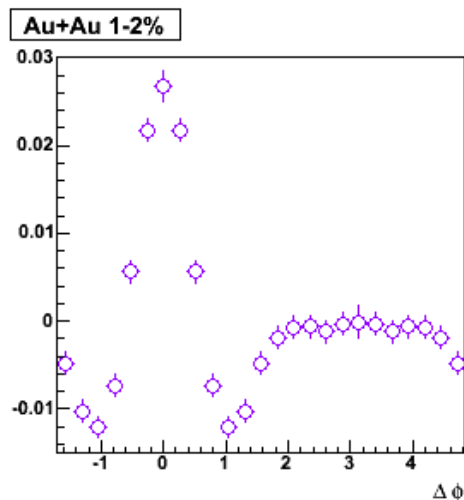
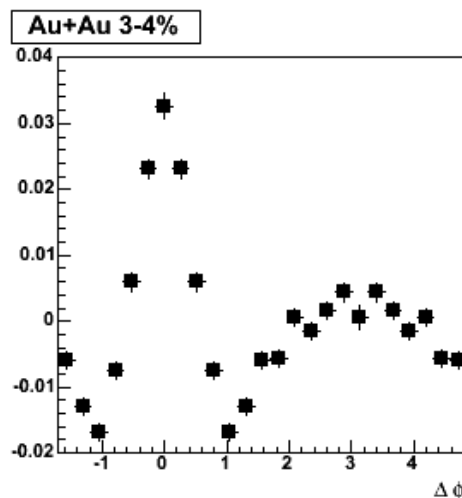
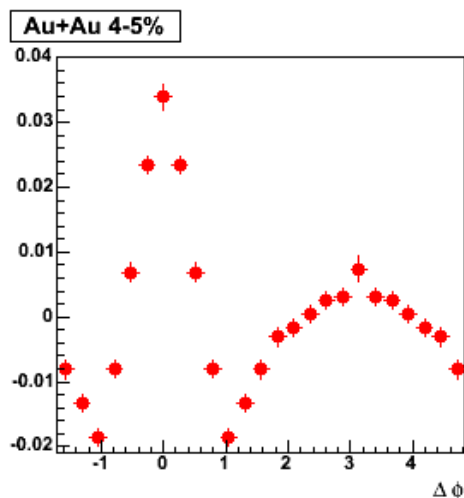


$$\frac{dN}{d\phi} \propto 1 + 2v_1 \cos \phi + 2v_1^s \sin \phi + 2v_2 \cos 2\phi + 2v_2^s \sin 2\phi + 2v_3 \cos 3\phi + \dots$$

$$\frac{dN}{d\phi} \propto 1 + \sum_{n=1}^{\infty} 2v_n \cos n(\phi - \psi_n) \Rightarrow \left\langle \frac{dN_{\text{pairs}}}{d\Delta\phi} \right\rangle^{(\text{flow})} \propto 1 + \sum_{n=1}^{\infty} 2 \langle v_n^2 \rangle \cos n(\Delta\phi)$$

# Centrality evolution of $\Delta\phi$ di-hadron projections

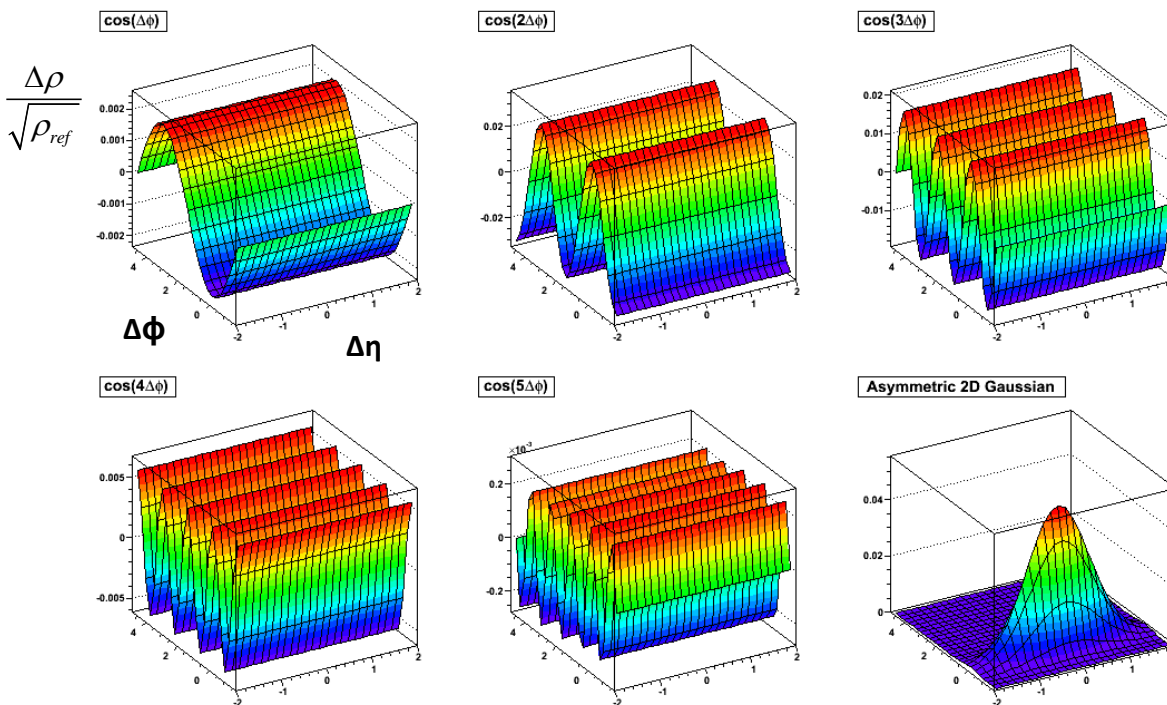
## - evidence for higher harmonics -





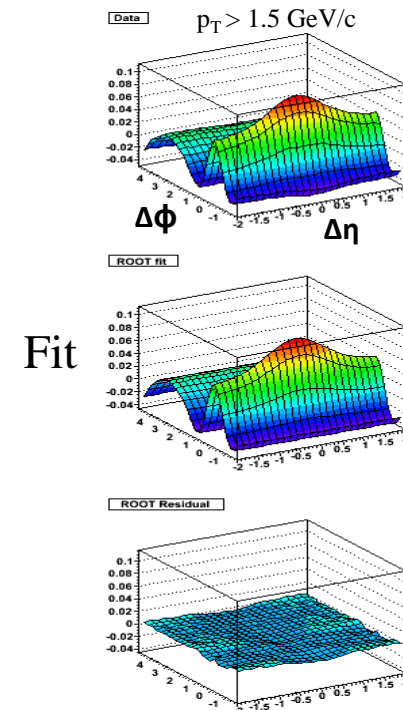
# Di-hadron correlation analysis

- applied to determine centrality and  $p_T$  dependence of long range correlations in  $\Delta\eta$ . Combined fit function for initial density fluctuations and medium modified jet (remainder):  $v_1$  to  $v_5$  plus 2d Gaussian.



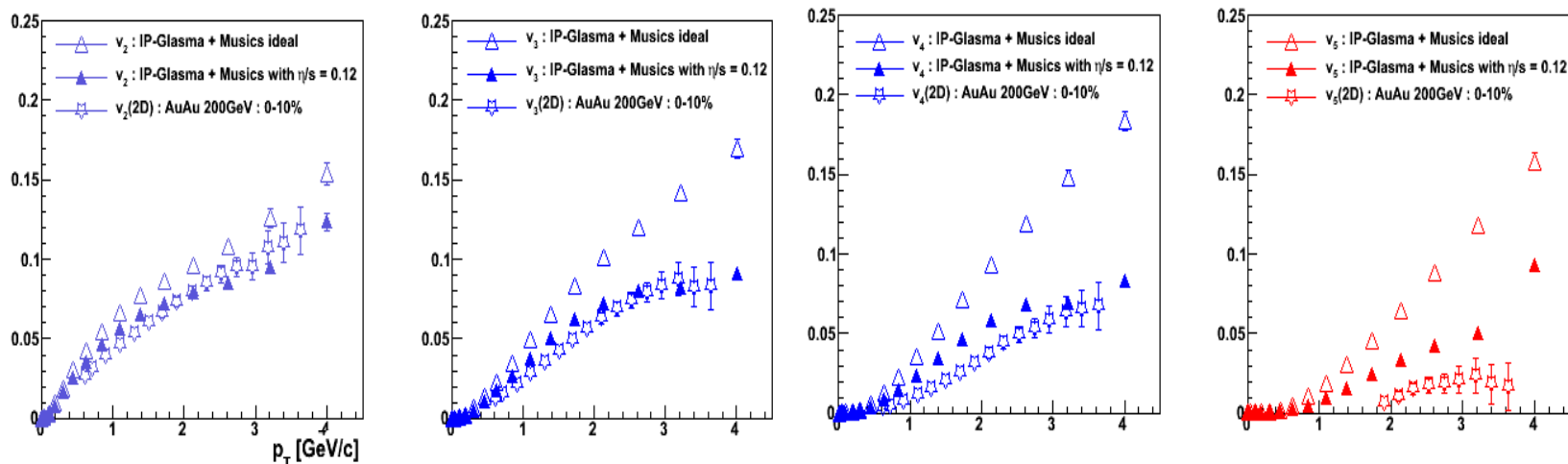
Data: STAR, 0=10%,

$p_T > 1.5$  GeV/c

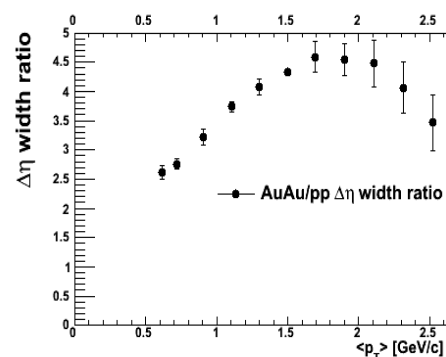
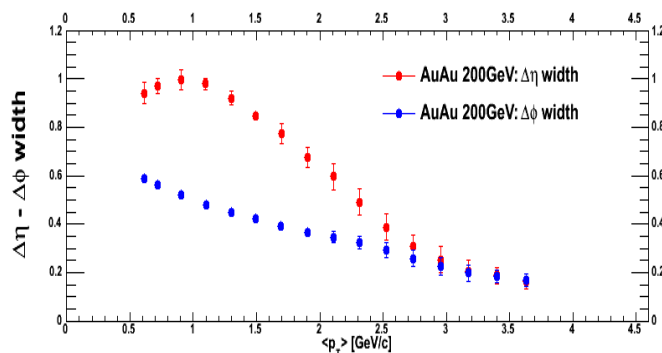


# Di-hadron correlations in STAR

- Major result on harmonics: sensitivity to viscosity



- Major result on remainder: jet medium modification



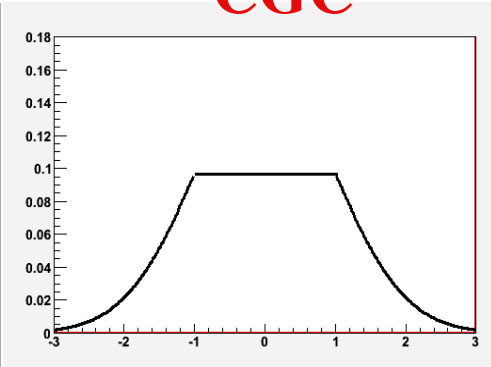
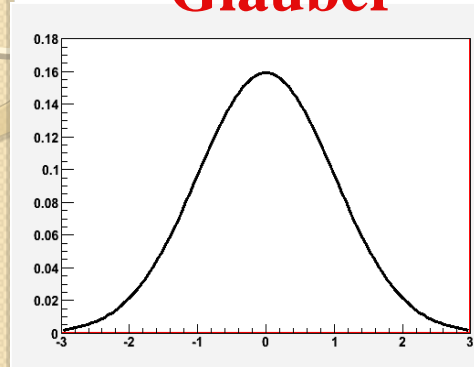


# Initial State determines flow strength

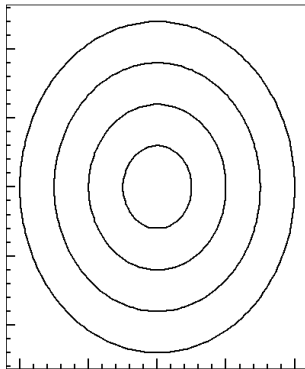
## Radial gluon distribution

### Glauber

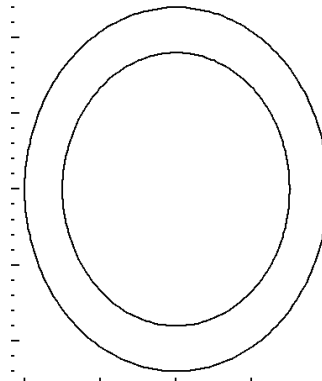
### CGC



## 2-D density profile

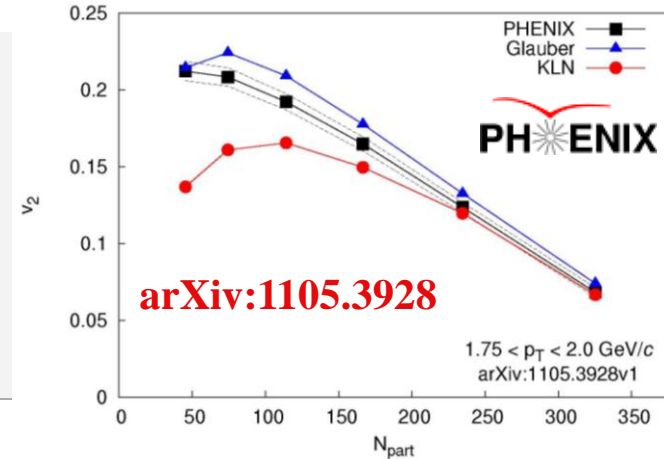


**Smaller eccentricity**

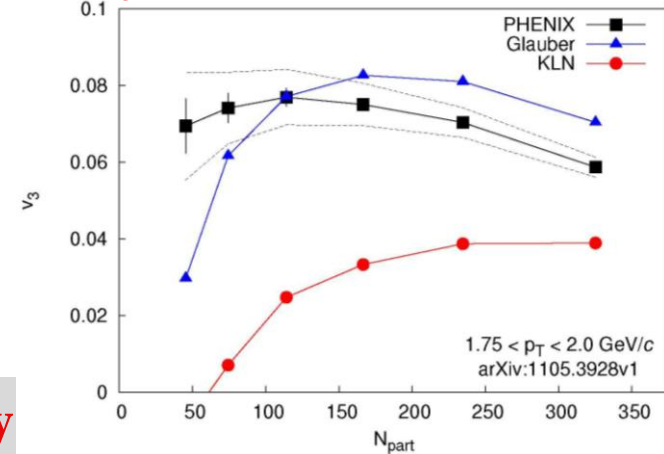


**larger eccentricity**

## $v_2$ described by Glauber and CGC



## $v_3$ described only by Glauber



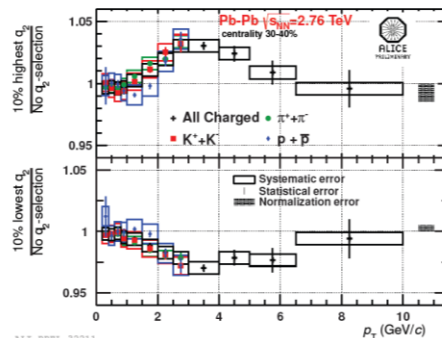
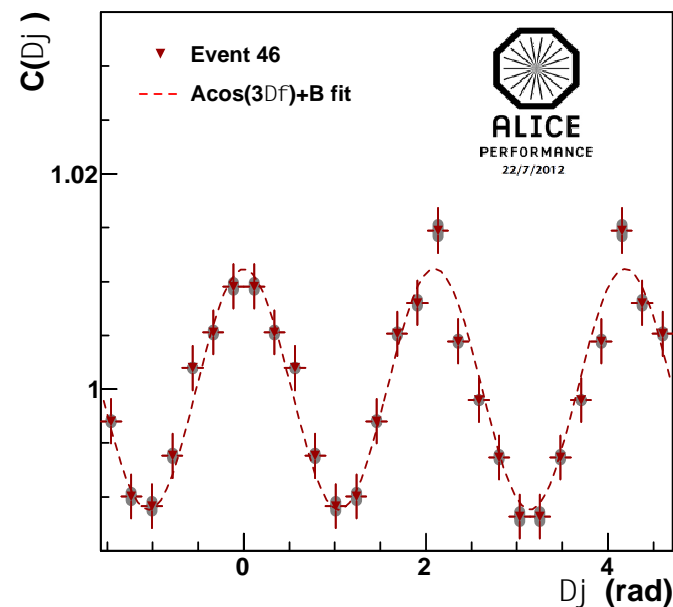
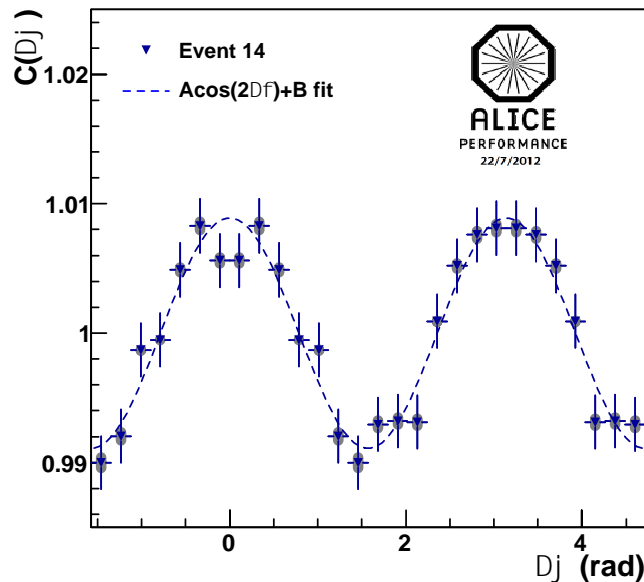
Theory calculation: Alver et al., PRC82,034913

**weak centrality dependence of  $v_3 \Rightarrow$  fluctuations origin**

# An exciting prospect for the future: Event engineering

- The e-by-e statistics at the LHC enable event classification on the basis of harmonics measurements. (PLB 719 (2013) 394)

Pb-Pb  $\sqrt{s_{NN}} = 2.76$  TeV, 4-5% central



- Future studies: explore fluctuations and multiplicity distributions e-by-e.

# Lattice QCD predictions for QCD transition

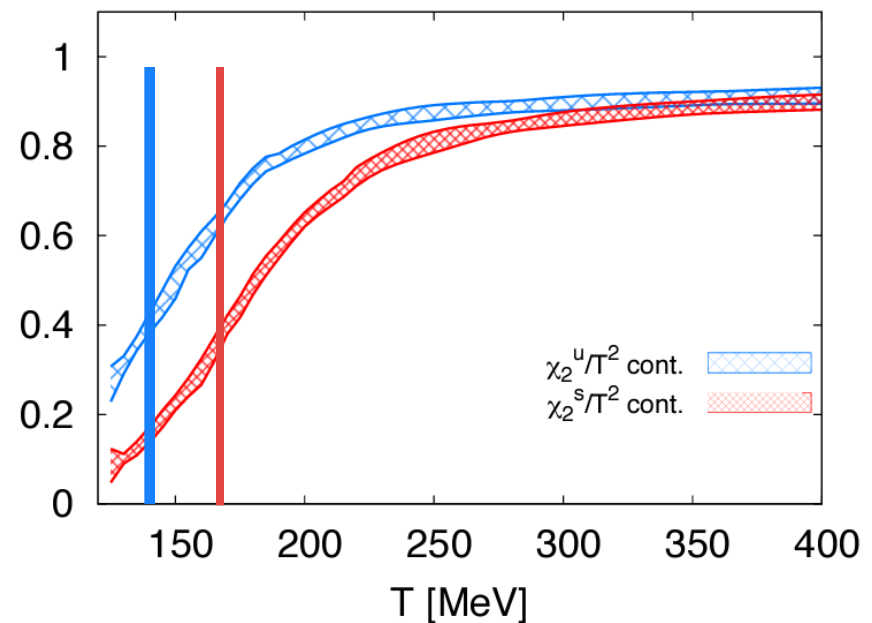
- Recent high resolution lattice calculations have yielded reliable continuum extrapolations for all relevant order parameters of the QCD phase transition.

## The conclusions are:

A.) that the transition is an analytic crossover for an extended range of temperatures ( $\Delta T$  around 100 MeV)

B.) that in the crossover region there might be indications of a flavor hierarchy during hadronization (heavier flavors freeze out at higher temperatures, more abundant if emission is statistical).

Difference between light and strange flavor



C. Ratti et al., PRD 85, 014004 (2012)  
R. Bellwied, arXiv:1205.3625

# A short primer on QCD susceptibilities

$$\Omega(T, \mu) \equiv \ln \mathcal{Z}(V, T, \mu) / VT^3$$

**Grand potential  
of QCD**

$$\frac{p_{SB}}{T^4} = \Omega^{(0)}(T, \mu) = \frac{8\pi^2}{45} + \sum_{f=u,d,..} \left[ \frac{7\pi^2}{60} + \frac{1}{2} \left( \frac{\mu_f}{T} \right)^2 + \frac{1}{4\pi^2} \left( \frac{\mu_f}{T} \right)^4 \right]$$

**Infinite T limit  
SB gas**

**First derivative of grand potential with respect to chemical potential is the density (density of quarks), equals zero at  $\mu=0$ .**

**Second derivative is susceptibility (variation of density with respect to infinitesimal change in chemical potential).**

$$\frac{\chi_{ff}(T, \mu)}{T^2} = \frac{\partial^2 \Omega(T, \mu)}{\partial (\mu_f/T)^2}, \quad \frac{\chi_{fk}(T, \mu)}{T^2} = \frac{\partial^2 \Omega(T, \mu)}{\partial (\mu_f/T) \partial (\mu_k/T)}$$

**Diagonal and  
non-diagonal  
susceptibilities**

**Fluctuation of system.**

**Correlation between conserved quantities**

$$\begin{aligned} \frac{\chi_{uu}(T, \mu_q)}{T^2} &= 2c_2^{uu} + 12c_4^{uu} \left( \frac{\mu_q}{T} \right)^2 + 30c_6^{uu} \left( \frac{\mu_q}{T} \right)^4 + \dots \\ \frac{\chi_{ud}(T, \mu_q)}{T^2} &= 2c_2^{ud} + 12c_4^{ud} \left( \frac{\mu_q}{T} \right)^2 + 30c_6^{ud} \left( \frac{\mu_q}{T} \right)^4 + \dots \end{aligned}$$

**Taylor  
expansion of  
susceptibilities**

# Susceptibility ratios in lattice QCD = higher moment ratios of multiplicity distribution

Susceptibility ratios proposed as a model independent measure of T<sub>ch</sub> at  $\mu=0$   
(arXiv:1202.4173)

$$\kappa_B \sigma_B^2 \equiv \frac{\chi_{4,\mu}^B}{\chi_{2,\mu}^B} = \frac{\chi_4^B(T)}{\chi_2^B(T)} \left[ \frac{1 + \frac{1}{2} \frac{\chi_6^B(T)}{\chi_4^B(T)} (\mu_B/T)^2 + \dots}{1 + \frac{1}{2} \frac{\chi_4^B(T)}{\chi_2^B(T)} (\mu_B/T)^2 + \dots} \right]$$

At  $\mu=0$ : higher order expansion terms are zero, therefore  $\chi_2 \sim c_2, \chi_4 \sim c_4, \chi_6 \sim c_6$ , etc.

- The first four cumulants are

$$C_1 = \langle (\delta x) \rangle \quad C_2 = \langle (\delta x)^2 \rangle$$

$$C_3 = \langle (\delta x)^3 \rangle \quad C_4 = \langle (\delta x)^4 \rangle - 3 \langle (\delta x)^2 \rangle^2$$

- We can then define

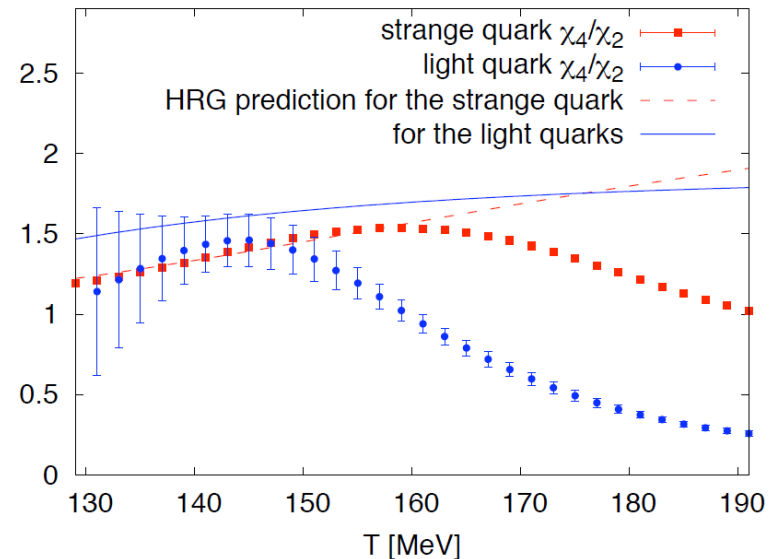
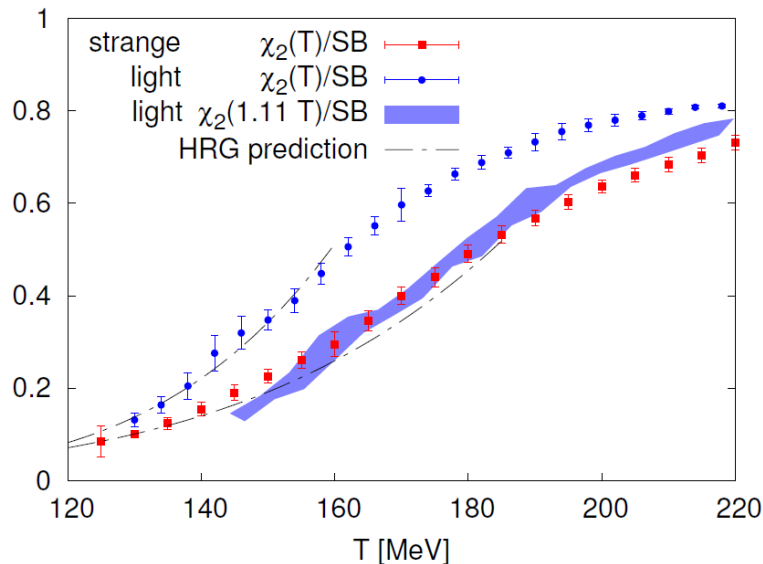
$$\text{Variance: } \sigma^2 = C_2 \quad \text{Standard deviation: } \sigma = \sqrt{C_2}$$

$$\text{Skewness: } S = C_3 / C_2^{3/2} \quad \text{Kurtosis: } \kappa = C_4 / C_2^2$$

$$S\sigma = C_3 / C_2 \quad \kappa\sigma^2 = C_4 / C_2$$

# Most recent results

- Latest results are based on continuum extrapolations of flavor dependent higher order susceptibility ratios and signal a flavor hierarchy in the QCD crossover region (Bellwied et al., arXiv:1305.6297)



- Analysis of PID higher moments in ALICE and STAR has started.
- $\kappa\sigma^2 = \chi_4/\chi_2$  is a good thermometer for hadronization.
- Strong fluctuations in  $\kappa\sigma^2$  for net-charge (charge number) and net-protons (baryon number) as a function of energy might also indicate critical point in phase diagram.

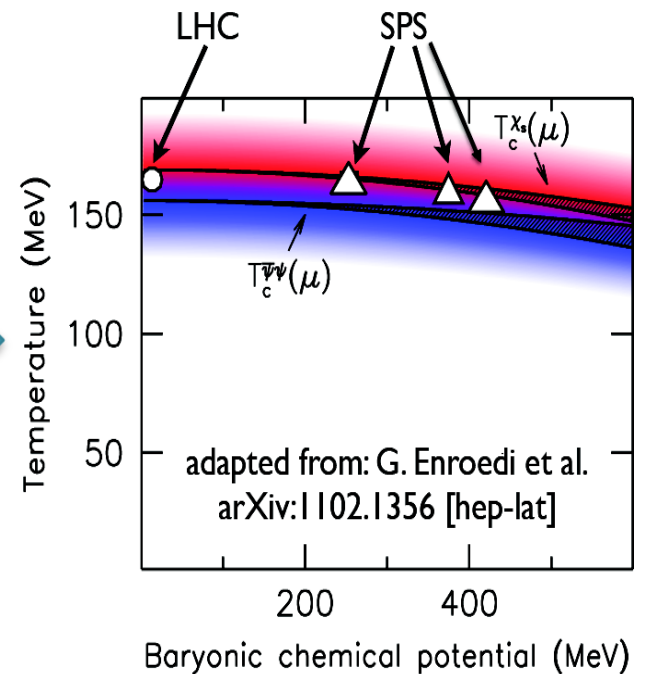
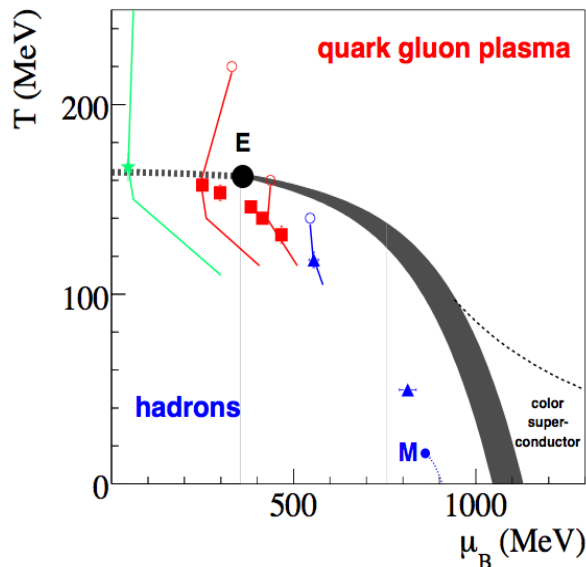




# Alternate explanation: non-equilibrium proton annihilation after hadronization

Idea based on enhanced in-medium annihilation cross sections in hadronic transport codes, e.g. UrQMD

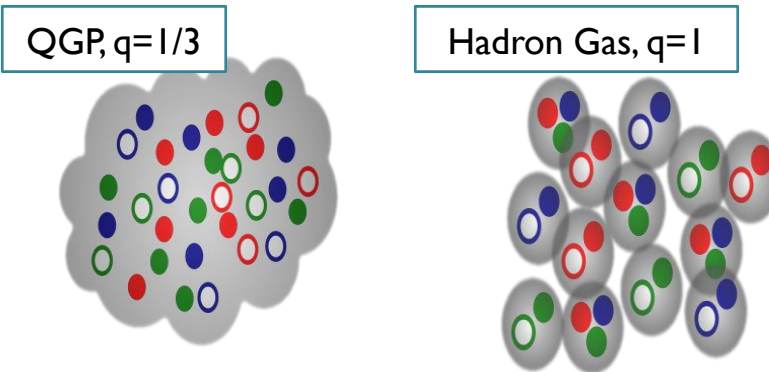
- Steinheimer, Aichelin, Bleicher, *arXiv:1203.5302*
- Karpenko, Sinyukov, Werner, *arXiv:1204.5351*
- Becattini et al., *arXiv:1201.6349*



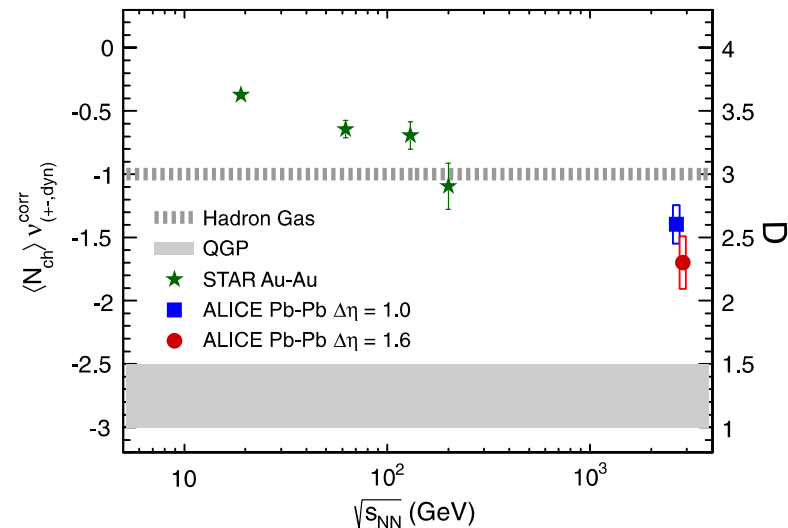
# Charge fluctuations

$$n_{(+,-,dyn)} = \frac{\langle N_+(N_+ - 1) \rangle}{\langle N_+ \rangle^2} + \frac{\langle N_-(N_- - 1) \rangle}{\langle N_- \rangle^2} - 2 \frac{\langle N_+ N_- \rangle}{\langle N_+ \rangle \langle N_- \rangle}$$

- e-by-e net charge fluctuations depend on charge carriers
- PRL 110, 152301 (2013)



*Jeon, Koch, PRL 85, 2072 (2000).*  
*Asakawa et al., PRL 85, 2076 (2000).*

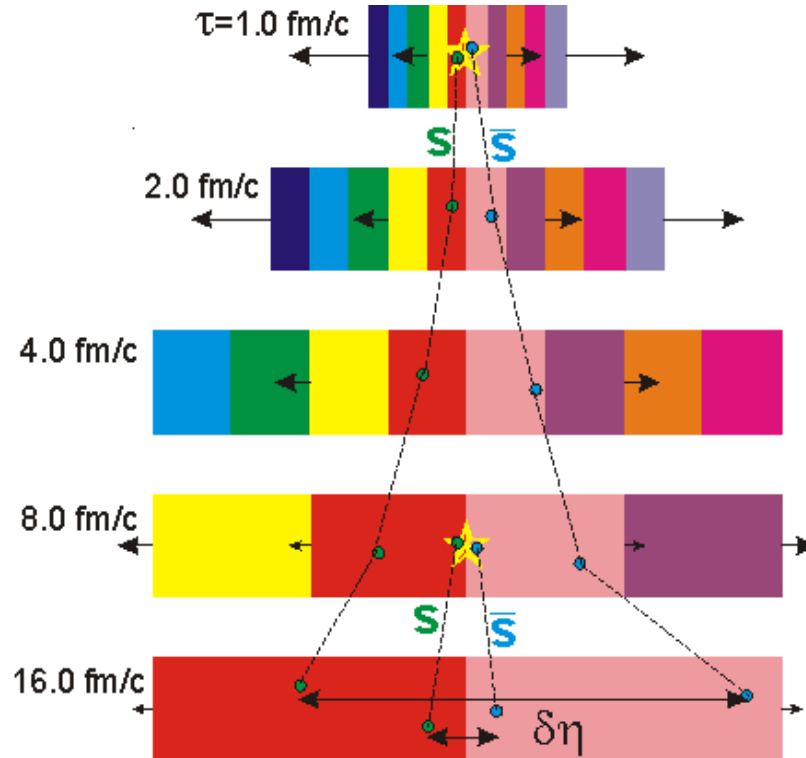


- Small value in ALICE consistent with onset of partial charge carriers

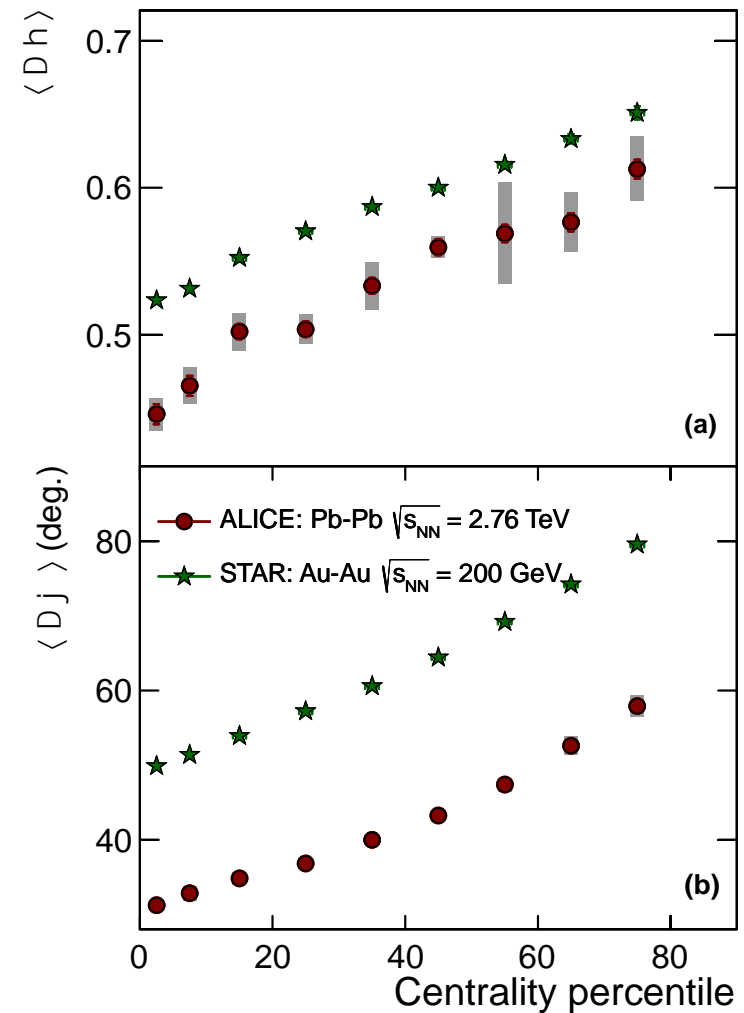
# Balance function

$$B(Dh) = \frac{1}{2} \left\{ \frac{N_{+-}(Dh) - N_{++}(Dh)}{N_+} + \frac{N_{-+}(Dh) - N_{--}(Dh)}{N_-} \right\}$$

- correlation of balancing charges depends on hadronization time
- PLB 723 (2013) 267



*Bass, Danielewicz, Pratt, PRL 85, 2689 (2000).*

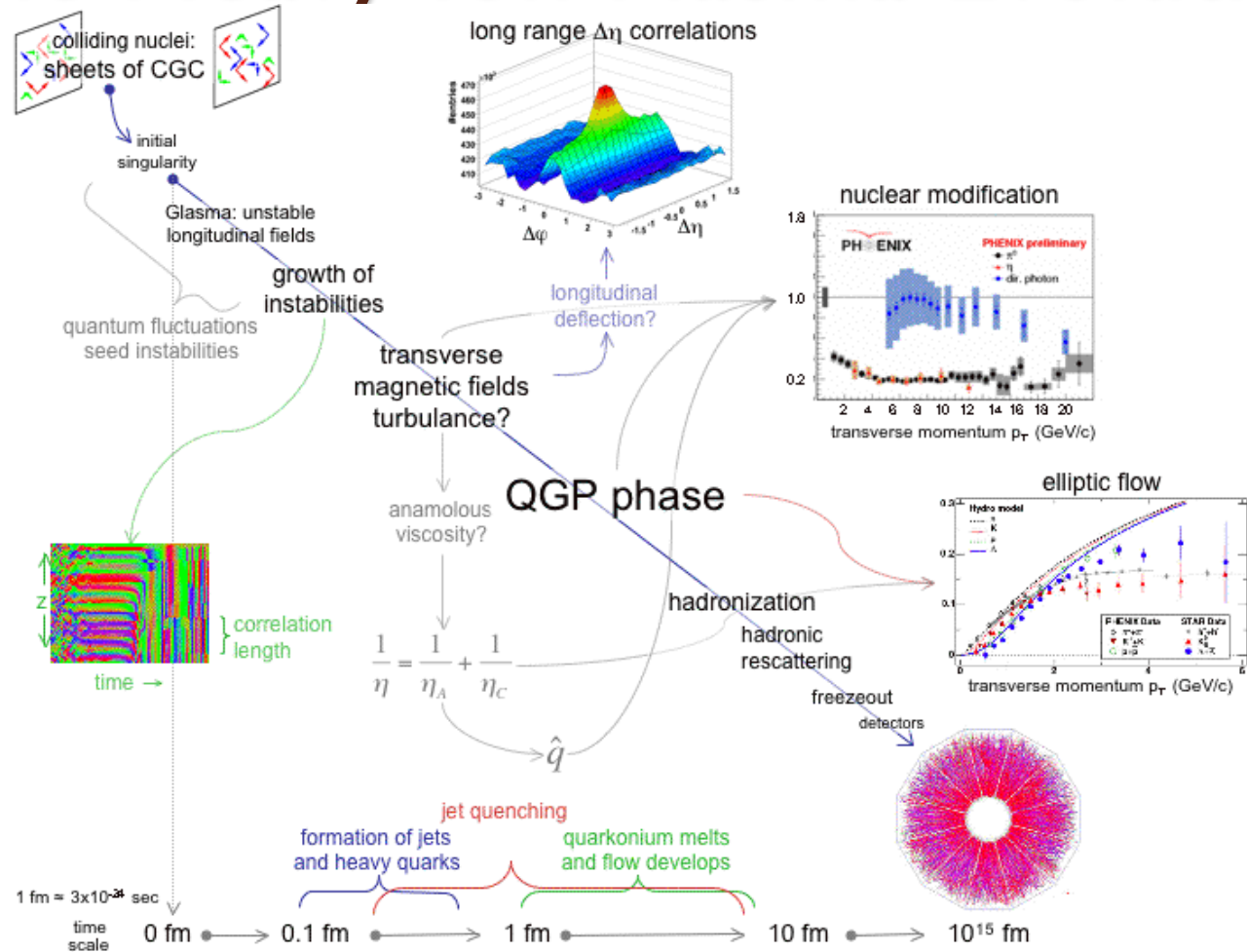


- Decrease in width consistent with increase in  $\tau_{had}$

# L3, Part 2: Conclusions / Future



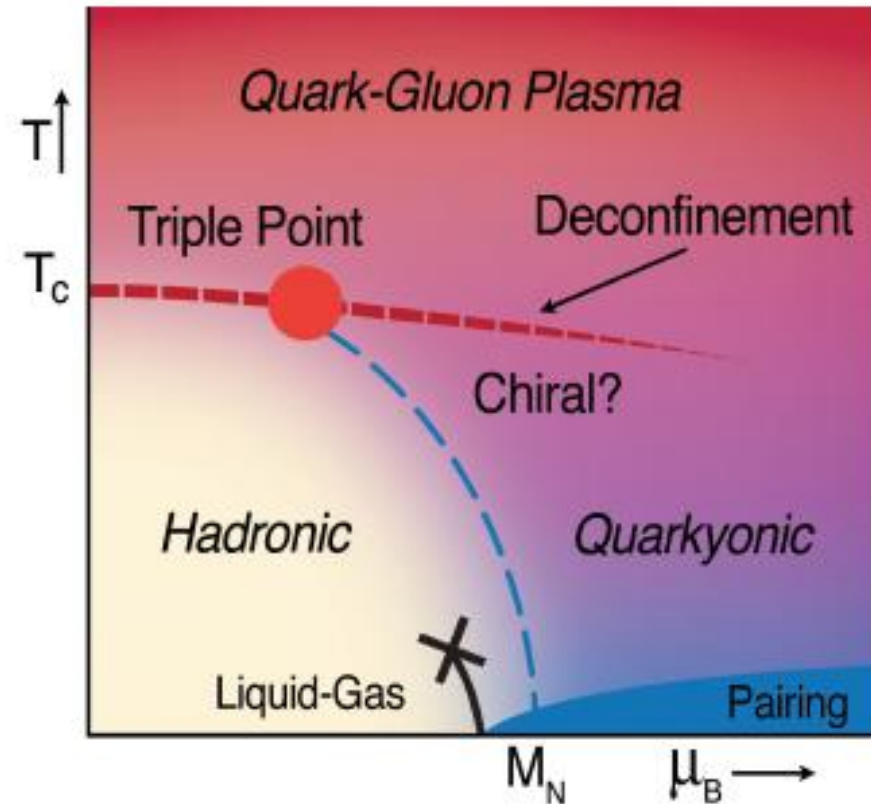
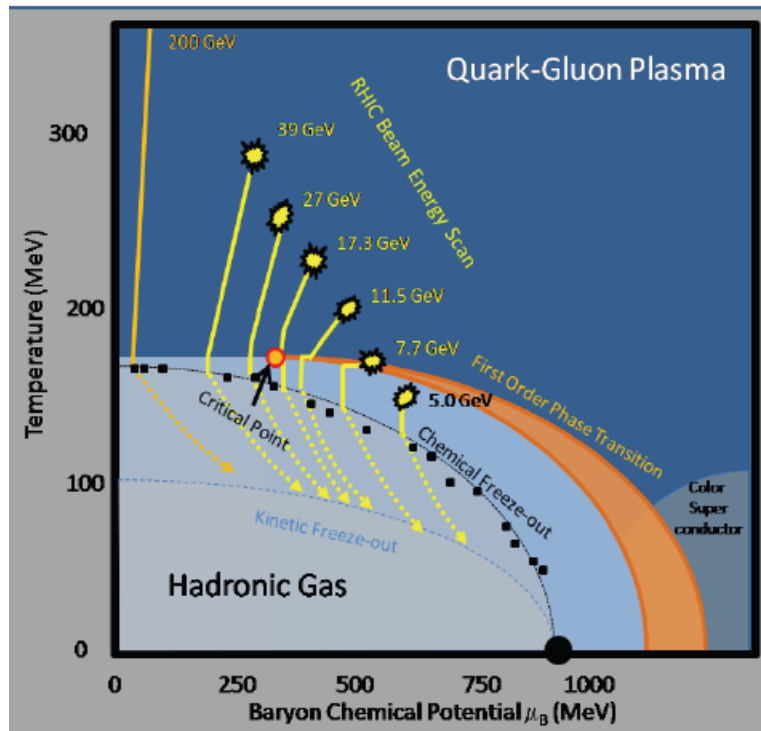
# The Heavy Ion Plasma Evolution



Coherent story except for early thermalization and strong coupling near the transition which cannot be easily reconciled with pQCD

# Where does it all begin / end ?

## Energy dependence of QCD matter

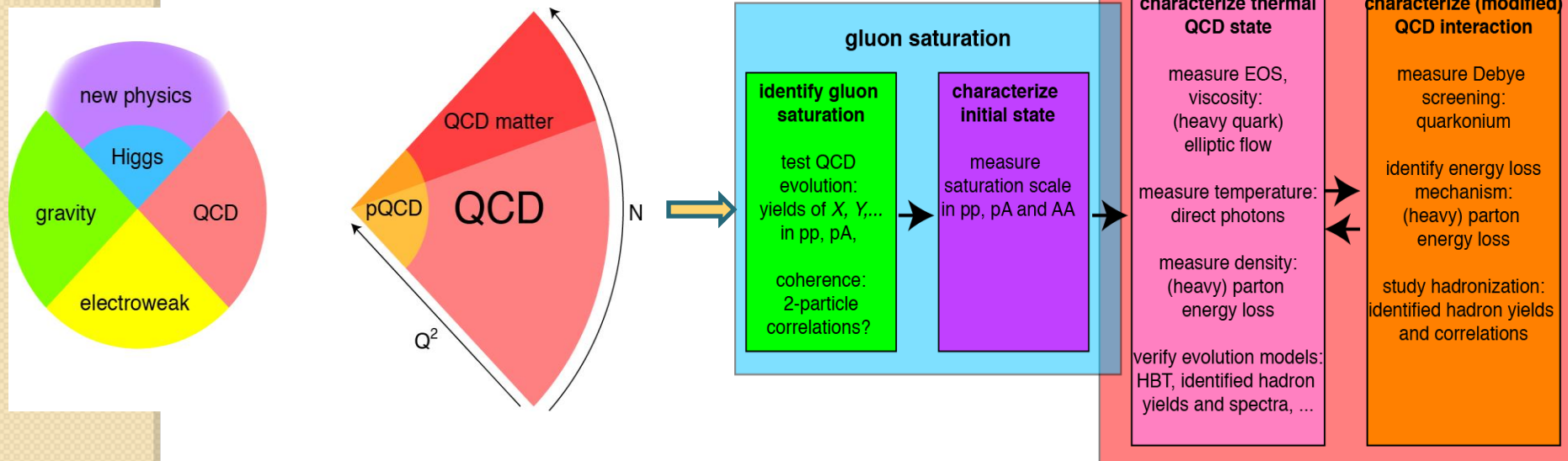


The future: high energy at LHC, low energy at FAIR / RHIC

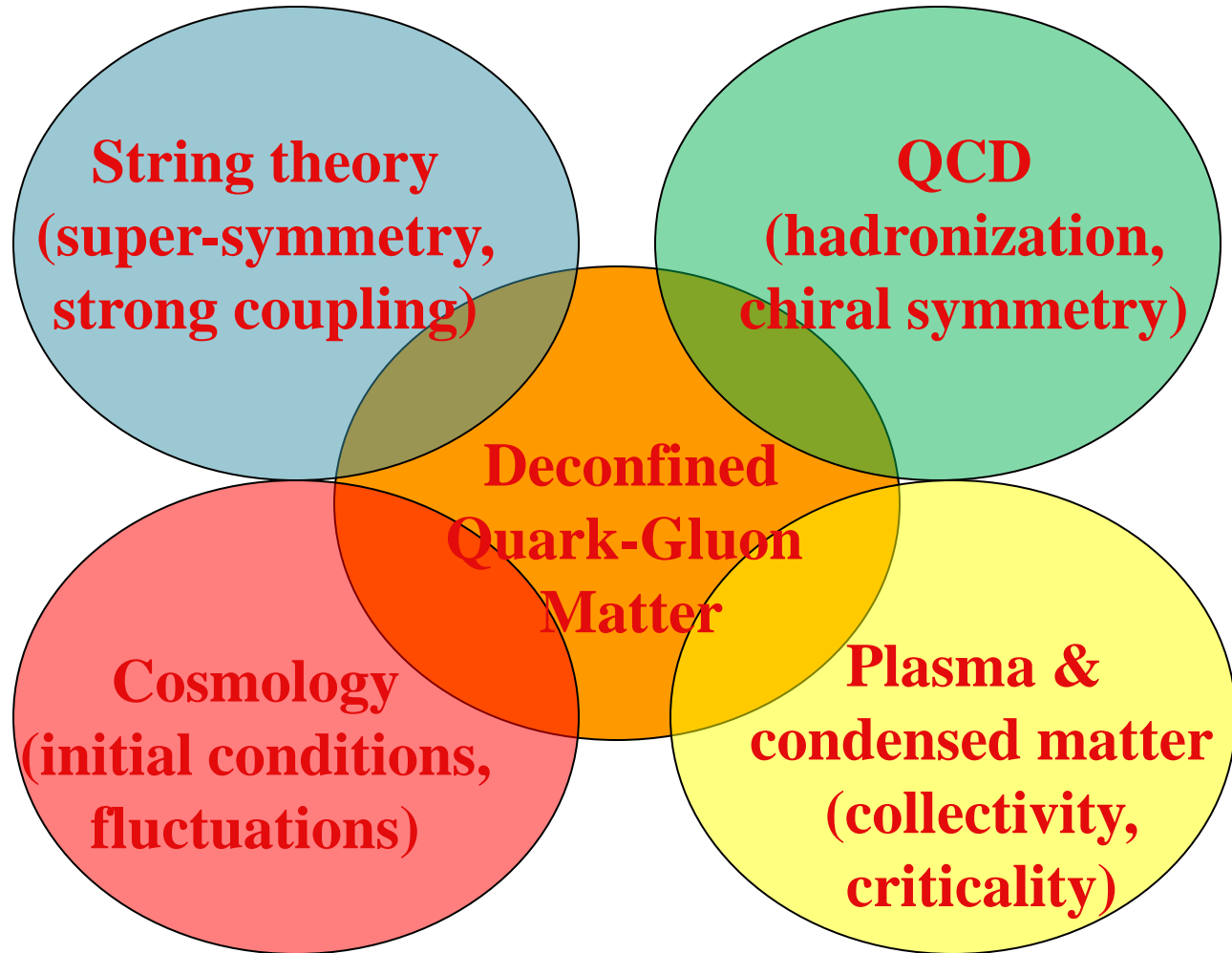


# The lesson from RHIC for high T QCD matter: focus on the difference between medium and vacuum

- QCD matter may be more weakly interacting at very high T, *but will not be described by pQCD in the original sense.*
- QCD case is not just an analogy to classical thermodynamics, there will be *new emergent phenomena*
  - Strong modification of coupling (interaction strength) and mass at high T
  - Matter formation in medium and vacuum (hadronization) ?
  - Properties of liquid phase / mixed phase



# Relativistic Heavy Ion Collisions have come a long way



# Suggestions for further reading

- **QCD: The Modern Theory of the Strong Interaction**  
F. Wilczek, *Ann. Rev. Nucl. Part. Sci.* 32 (1982) 177
- **Symmetry breaking and quark confinement**, *Concepts of Particle Physics Vol I and II*, K. Gottfried and V.F. Weisskopf, Oxford Press (1984)
- **The first second of the universe**  
D.J. Schwarz, *arXiv:astro-ph/0303574*
- **The phase diagram of QCD**  
S. Hands, *arXiv:physics/0105022*
- **String Theory and the Quark Gluon Plasma**  
M. Natsuume, *arXiv:hep-ph/0701201*
- **Transition from Hadron Matter to Quark-Gluon Plasma**  
H. Satz, *Ann. Rev. Nucl. Part. Sci.* 35 (1985) 245
- **The Search for the Quark-Gluon Plasma**  
J. Harris and B. Muller, *Ann. Rev. Nucl. Part. Sci.* 46 (1996) 71